













# The Ferm "Robotics": 1941



Isaac Asimov used the word Robotics in his short SF story, *Liar!*, published in





Assessment Exercise 2014							
Cost Centre	Institution	Number of eligible staff	Percentage of research activity judged to meet the standard of :				
			4 star	3 star	2 star	1 star	unclassified
18 electronic engineering	CityU	52	4	44	41	11	0
	HKBU						
	LU			-			
	CUHK	36	21	42	31	2	4
	HKIEd			-	-		-
	PolyU	27	5	41	37	10	7
	HKUST	40	16	58	24	1	1
	HKU	36	7	47	35	6	5
	Sector-wide	191	10	47	34	6	3
1							





A Brief History on Industrial Robot Control













## Robot Manipulator Dynamics

Robot manipulator dynamics:

 $M(\Theta)\ddot{\Theta} + V(\Theta,\dot{\Theta}) + G(\Theta) = au$ 

where

 $M \in R^{n imes n}$ , a symmetric, PD mass matrix  $V \in R^{n imes 1}$ , a vector containing all the velocity terms  $G \in R^{n imes 1}$ , a vector containing gravity term

 $au \in R^{n imes 1}$  , the joint torque vector

 $\Theta \in R^{n imes 1}$  , the joint position vector

n is the degree of freedom of the robot

Obviously, it is a second-order non-linear matrix equation.

## PD Control

Objective:  $\Theta_d = \dot{\Theta}_d = \Theta_d = 0$ Dynamics:  $M(\Theta)\Theta + V(\Theta, \dot{\Theta}) + G(\Theta) = \tau$ Control:  $\tau = K_p(\Theta_d - \Theta) + K_v(\dot{\Theta}_d - \dot{\Theta}) = -K_p\Theta - K_v\dot{\Theta}$ Lyapunov function:  $V = \frac{1}{2}\dot{\Theta}^T M(\Theta)\dot{\Theta} + \frac{1}{2}\Theta^T K_p\Theta + \phi(\Theta)$ and we then have:  $\dot{V} = -\dot{\Theta}^T K_v\dot{\Theta} < 0$ and we then have:  $\dot{\Theta} = 0 \Rightarrow \ddot{\Theta} = 0$ , from the s.s. analysis,  $K_p\Theta + G(\Theta) = 0 \Rightarrow \Theta_{ss} = -K_p^{-1}G(\Theta) \propto -\frac{1}{K_p}$ Smaller  $\Theta_{ss}$  requires larger  $K_p$  (larger capacity motors)!







## Robot Manipulator Dynamics

The robot dynamics:

 $M(\Theta)\ddot{\Theta} + V(\Theta,\dot{\Theta}) + G(\Theta) = \tau$ 

can be expressed as a linear regressor equation as follows:

 $M(\Theta)\ddot{\Theta}+V(\Theta,\dot{\Theta})+G(\Theta)=Y(\Theta,\dot{\Theta},\ddot{\Theta})p$  where

 $Y(\Theta, \dot{\Theta}, \ddot{\Theta}) \in \mathbb{R}^{n imes m}$ , is a known, regressor matrix  $p \in \mathbb{R}^{m imes 1}$ , a vector of all the dynamics parameters m is the number of robot dynamics parameters **Implementable Adaptive Control** Dynamics:  $M(\Theta)\ddot{\Theta} + V(\Theta, \dot{\Theta}) + G(\Theta) = \tau$ Control:  $\tau = \hat{M}(\Theta)\ddot{\Theta}^* + \hat{V}(\Theta, \dot{\Theta}) + \hat{G}(\Theta) = \hat{Y}(\Theta, \dot{\Theta}, \ddot{\Theta}^*)\hat{\rho}$ where  $\ddot{\Theta}^* = \ddot{\Theta}_d + K_v \dot{E} + K_p E$  and  $E = \Theta_d - \Theta$ Lyapunov function:  $V = E^T P E + \tilde{\rho}^T \Gamma^{-1} \tilde{\rho}$ and we then have:  $\dot{V} = -E^T Q E, Q > 0$ and with the parameter adaptation law defined as  $\dot{\rho} = -\Gamma Y^T(\Theta, \dot{\Theta}, \ddot{\Theta}) \hat{M}^{-1}(\Theta) B^T P E$ The above offers a practical and stable robot adaptive control!





#### Slotine-Li Adaptive Control\*

Dynamics:  $M(\Theta)\ddot{\Theta} + V(\Theta, \dot{\Theta}) + G(\Theta) = \tau$ Control:  $\tau = \hat{M}(\Theta)\ddot{\Theta}_r + \hat{V}(\Theta, \dot{\Theta})\dot{\Theta}_r + \hat{G}(\Theta) - Ks$ where  $s = \dot{\Theta} - \dot{\Theta}_r$  and  $\dot{\Theta}_r = \dot{\Theta}_d + \Lambda(\Theta_d - \Theta)$ Lyapunov function:  $V = \frac{1}{2}s^T M(\Theta)s + \tilde{\rho}^T \Gamma^{-1}\tilde{\rho}$ and we then have:  $\dot{V} = -\lambda s^T M(\Theta)s < 0$ and with the parameter adaptation law defined as  $\dot{\rho} = -\Gamma Y^T(\Theta, \dot{\Theta}, \dot{\Theta}_r, (\ddot{\Theta}_r - \lambda s))s$ The above offers a (theoretical) stable robot adaptive control! \* JE Slotine and W Li, "Adaptive manipulator control: a case study," in Proc. of IEEE ICRA 1987, pp. 1392-1400.



# **PD** plus Gravity Compensation Objective: $\Theta_d = c \Rightarrow \dot{\Theta}_d = \ddot{\Theta}_d = 0$ Dynamics: $M(\Theta)\ddot{\Theta} + V(\Theta, \dot{\Theta}) + G(\Theta) = \tau$ Control: $\tau = K_p E - K_v \dot{\Theta} + G(\Theta)$ where $E = \Theta_d - \Theta$ Lyapunov function: $V = \frac{1}{2} \dot{\Theta}^T M(\Theta) \dot{\Theta} + \frac{1}{2} E^T K_p E$ and we then have: $\dot{V} = -\dot{\Theta}^T K_v \dot{\Theta} < 0$ and we then have: $\dot{\Theta} = 0 \Rightarrow \ddot{\Theta} = 0$ , from the s.s. analysis, $K_p E = 0 \Rightarrow E = 0 \Rightarrow \Theta = \Theta_d$

With gravity compensation, no ss error, but require  $G(\Theta)$ !













Nervous System All perception involves signals in the nervous ødør system, which in turn malecu result from physical or chemical stimulation of ear the sense organs.









Thank You!

My sincere gratitude to all of my students and research associates, past and present, for their inspiration and contributions to this talk!