

Networked Cyber-Physical Systems (Net-CPS)

网络 信息-物理 融合 系统

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谢谢**CCC**组委会的邀请

谢谢各位到来

I have been in Chengdu before!



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Networked Cyber-Physical Systems

Infrastructure / Communication Networks

Internet / WWW
MANET

Sensor Nets

Robotic Nets

Hybrid Nets:
Comm, Sensor,
Robotic and
Human Nets

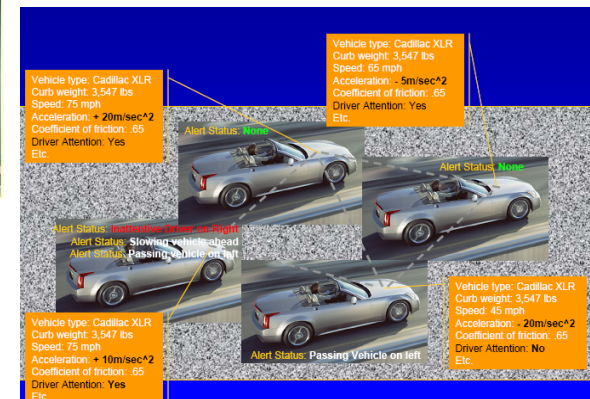
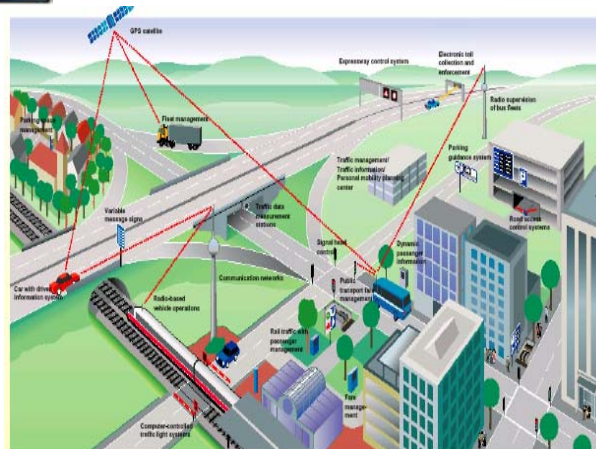
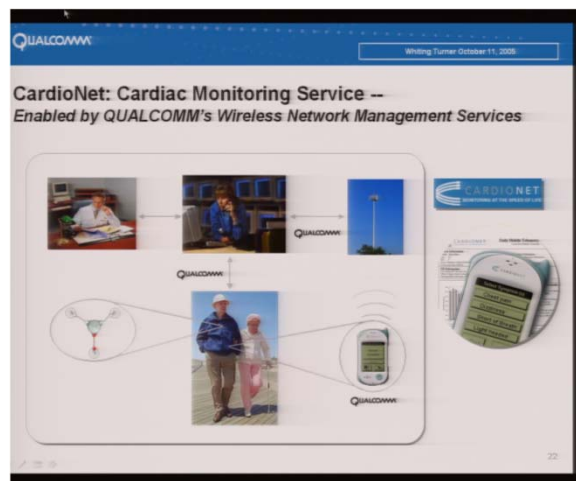
Social / Economic Networks

Social
Interactions
Collaboration
Social Filtering
Economic
Alliances
Web-based
social systems

Biological Networks

Community
Epidemic
Cellular and
Sub-cellular
Neural
Insects
Animal Flocks

Net-CPS: Wireless and Networked Embedded Systems



iPhone -- Smartphone



Future “Smart” Homes and Cities

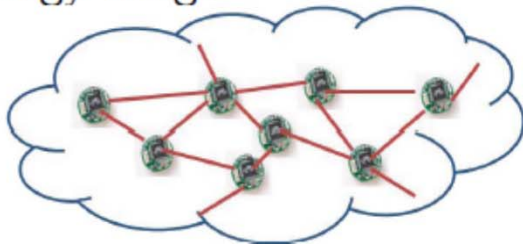
- UI for “Everything”
 - Devices with Computing Capabilities & Interfaces
- Network Communication
 - Devices Connected to Home Network
- Media: Physical to Digital
 - MP3, Netflix, Kindle eBooks, Flickr Photos
- Smart Phones
 - Universal Controller in a Smart Home
- Smart Meters & Grids
 - Demand/Response System for “Power Grid”
- Wireless Medical Devices
 - Portable & Wireless for Real-Time Monitoring



Net-CPS: Wireless Sensor Networks Everywhere

Wireless Sensor Networks (WSN) for infrastructure monitoring

- Environmental systems
- Structural health
- Construction projects
- Energy usage



Bridges



Snowpack



Soil liquefaction



Smart buildings

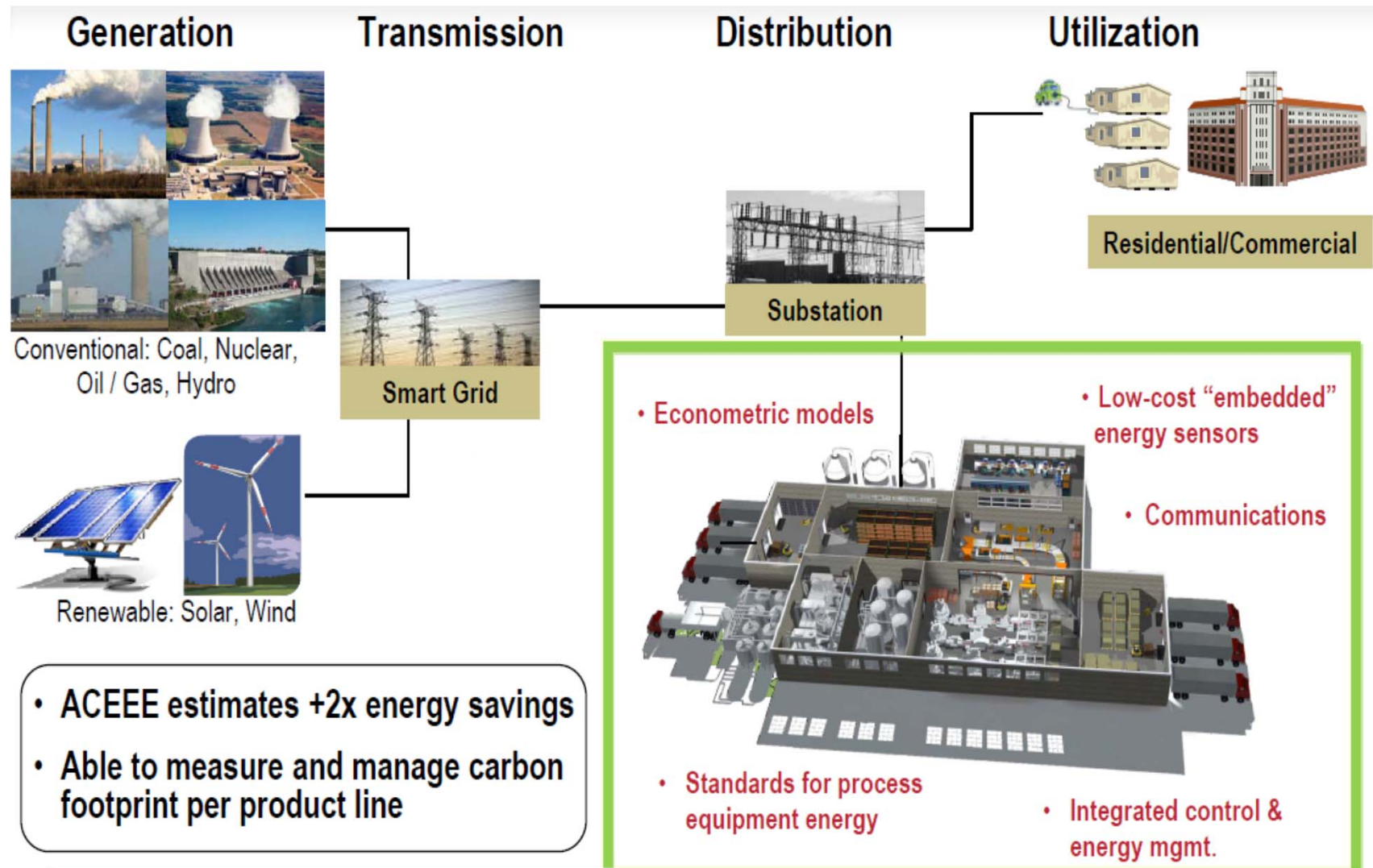


Traffic

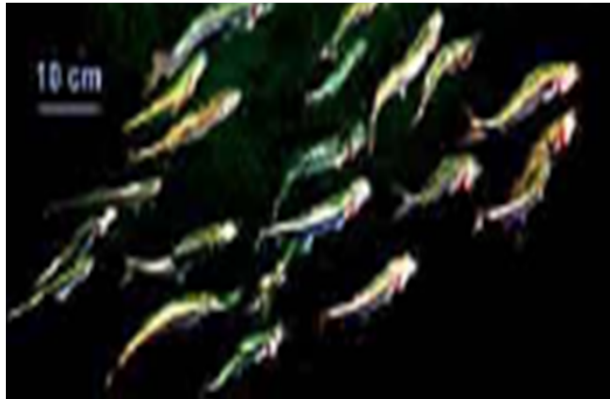


Vineyards

Net-CPS: Smart Grids



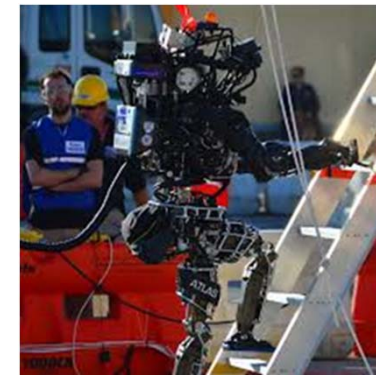
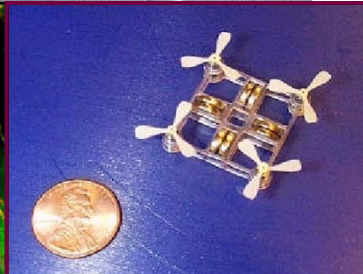
Net-CPS: Biological Swarms



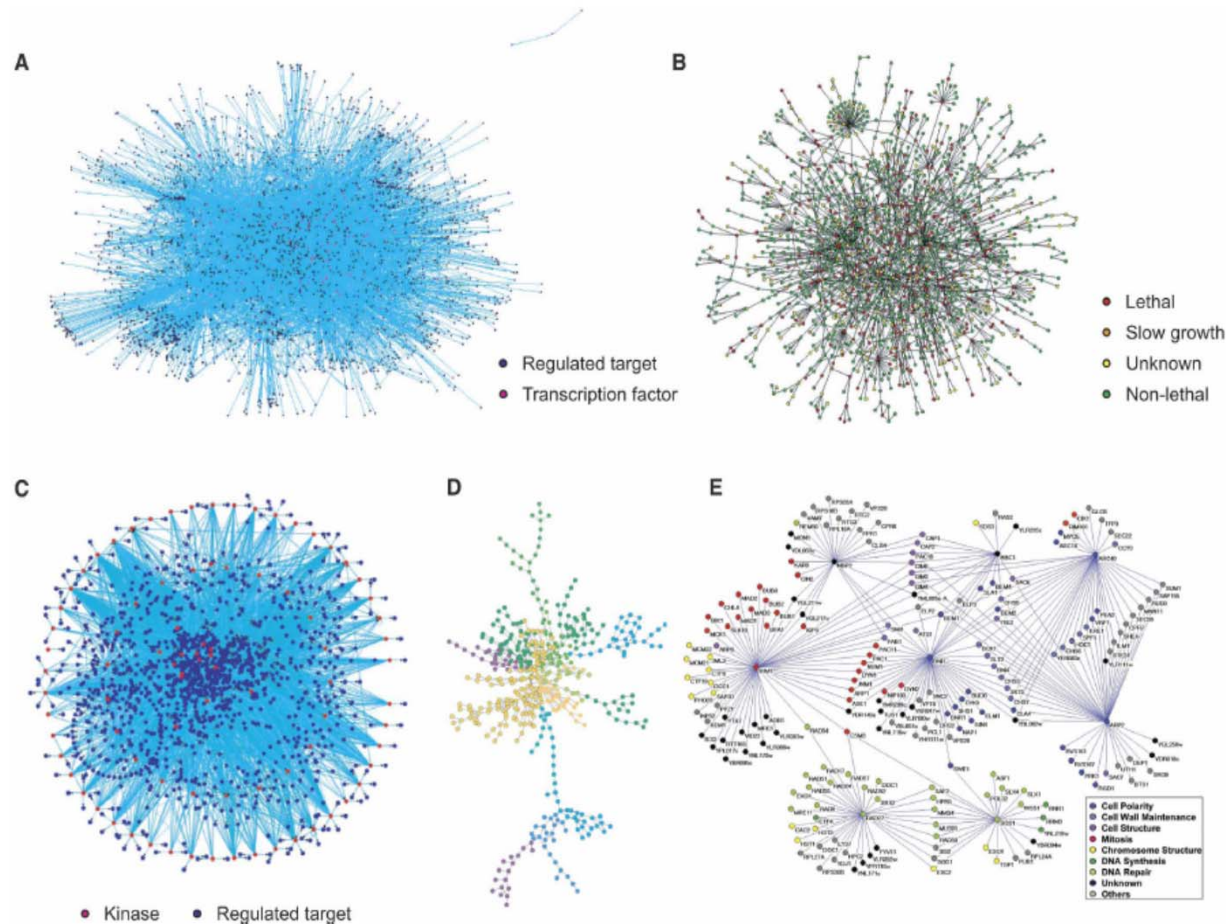
Net-CPS: Collaborative Autonomy



- **Component-based Architectures**
- **Communication vs Performance Tradeoffs**
- **Distributed asynchronous**
- **Fundamental limits**



Net-CPS: Biological Network Types



Examples of biological networks: [A] Yeast transcription factor-binding network; [B] Yeast protein-protein interaction network; [C] Yeast phosphorylation network ; [D] *E. Coli* metabolic network ; [E] Yeast genetic network ; Nodes colored according to their YPD cellular roles [Zhu et al, 2007]

Net-CPS: Social and Economic Networks over the Web

- We are much more “social” than ever before
 - Online social networks (SNS) permeate our lives
 - Such new Life style gives birth to new markets
- Monetize the value of social network
 - Advertising - major source of income for SNS
 - Joining fee, donation etc.
 - ...
- Need to know the common features of social networks



CPS and Net-CPS

- **CPS: Technological systems where physical and cyber components are tightly integrated**
- **Examples: smart phones, smart sensors, smart homes, smart cars, smart power grids, smart manufacturing, smart transportation systems, human robotic teams, ...**
- **Most of modern CPS are actually networked: via the Internet or the cloud, or via special logical or physical networks**
- **Examples: modern factories, Industrie 4.0, modern enterprises, heterogeneous wireless networks, sensor networks, social networks over the Internet, Industrial Internet (IIC), the Internet of Things (IoT), ...**

- With networks **new fundamental challenges** emerge: network semantics and characteristics
- **Fundamental challenges on two fronts:**
 - (a) on the interface between cyber and physical components and their joint design and performance;
 - (b) on the implications of the networked interfaces and the collaborative aspects of these systems and their design and performance.
- Networked Cyber-Physical Systems (Net-CPS)
- **Additional challenge:** incorporation of humans in Net-CPS, as system components from start

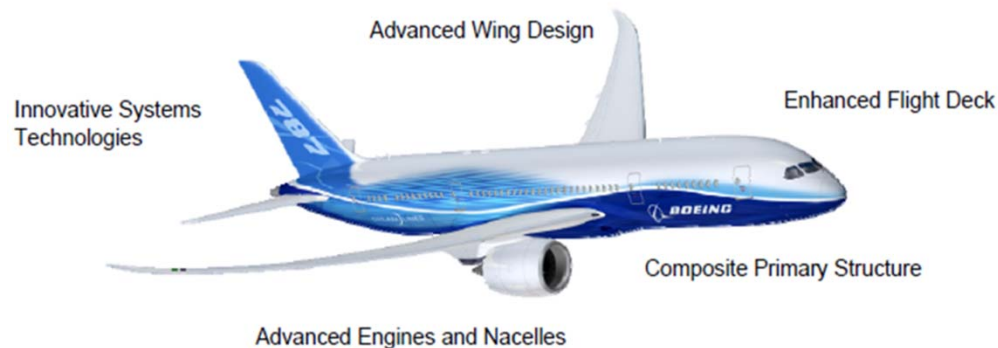
CPS Architecture: Materials-Geometry-Controls

The 787 Dreamliner delivers:

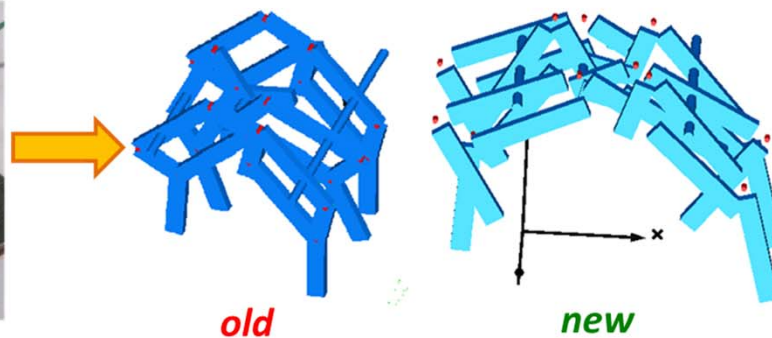
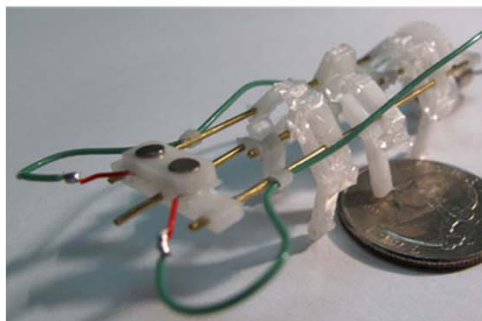
- 20%* reduction in fuel and CO₂
- 28% below 2008 industry limits for NO_x
- 60%* smaller noise foot print

*Relative to the 767

Composite wing – new control algorithms
All-electric platform – new aircraft VMS



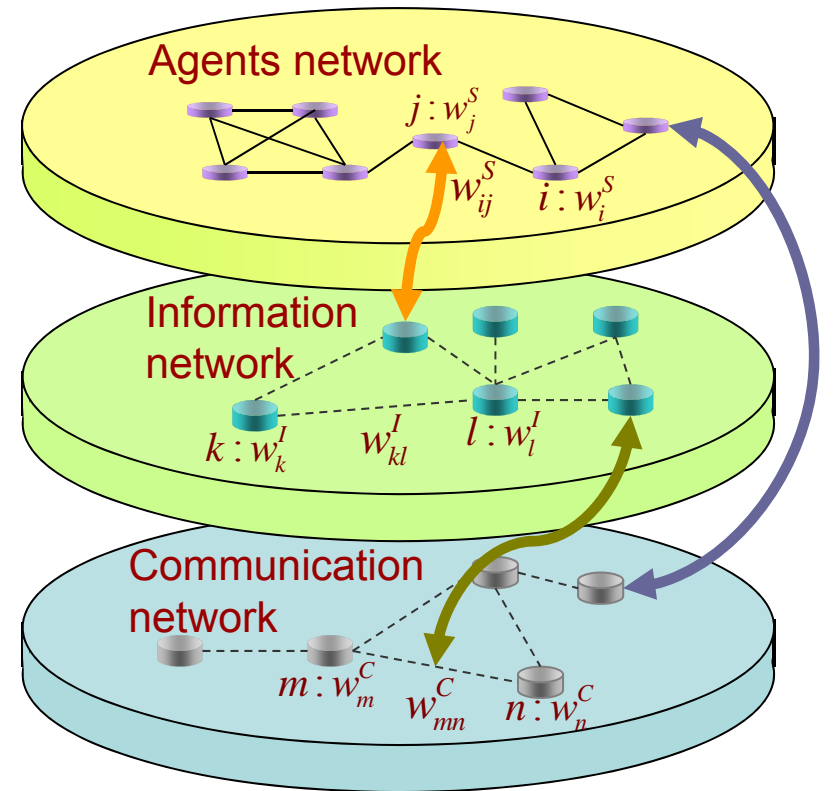
Architecture Logics,
their Representation
and Integration



Fast micro-robots –
new joint design
of geometry-
material-controls –
More stable and
faster running

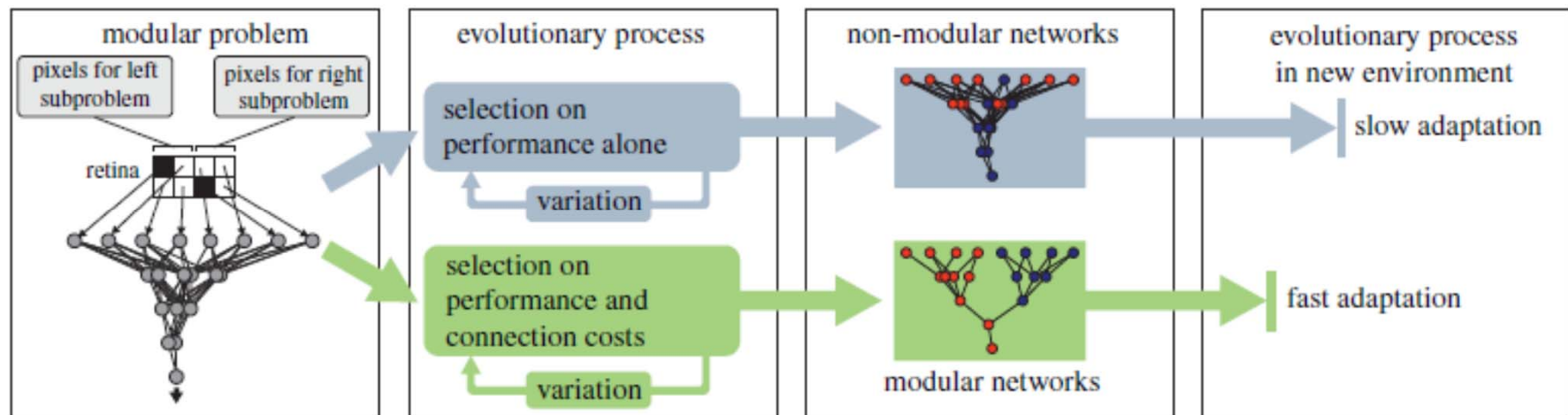
- **Multiple interacting coevolving multigraphs – three challenges**
- **Graph Topology Matters**
- **Networks and Collaboration – Constrained Coalitional Games**
- **Collaboration, Trust and Mistrust**
- **New Probabilistic Models**
- **Conclusions**

- Multiple Interacting Graphs
 - **Nodes**: agents, individuals, groups, organizations
 - Directed graphs
 - **Links**: ties, relationships
 - **Weights on links** : value (strength, significance) of tie
 - **Weights on nodes** : importance of node (agent)
- **Value directed graphs with weighted nodes**
- **Real-life problems: Dynamic, time varying graphs, relations, weights, policies**



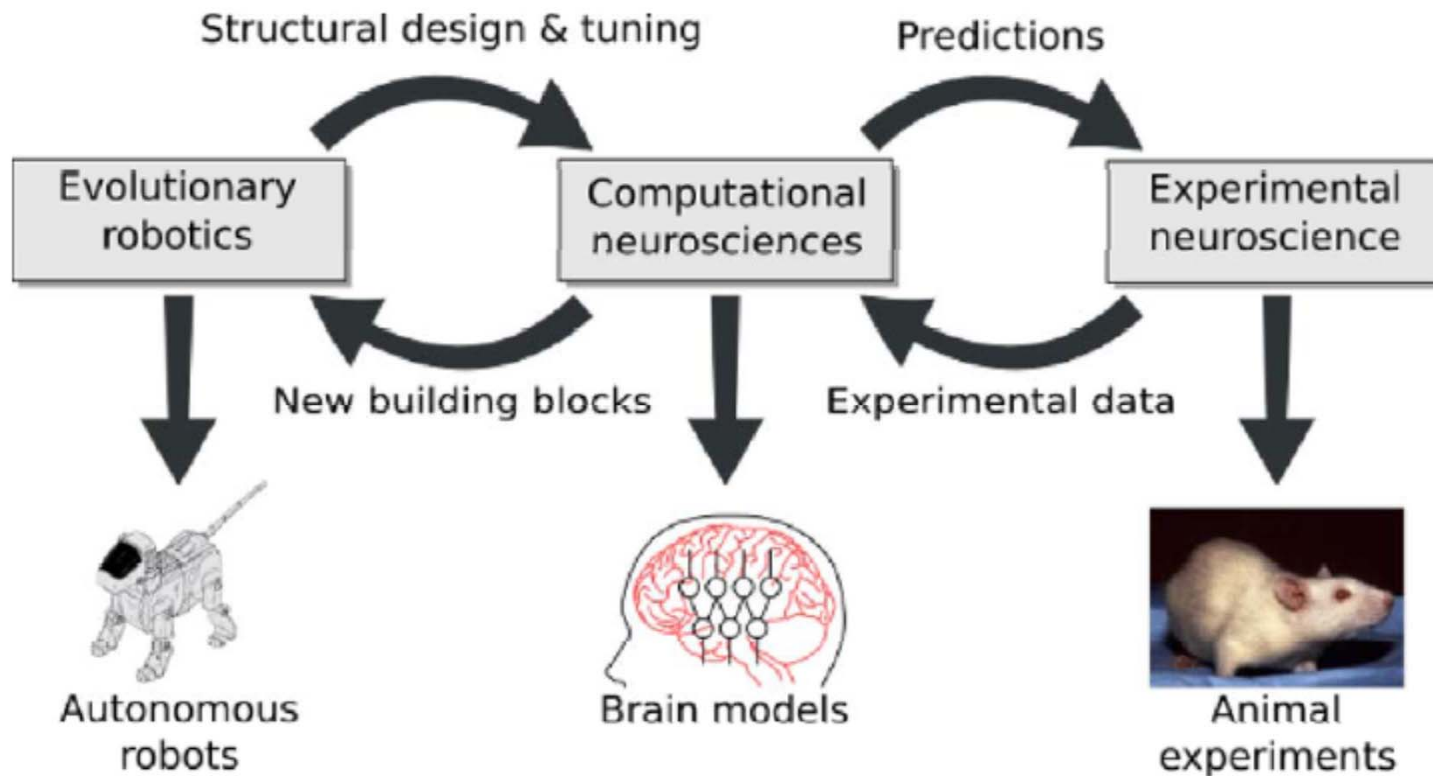
**Networked System
architecture & operation**

Challenges: Modularity vs Performance



- **Optimize only on performance – poor adaptivity**
- **Add cost of communications – improved adaptivity**
- **Communication motifs**
- **Evolvable modularity for some networked CPS?**

Neural Network Evolution: from programmed structure to function feedback on structure



Three Fundamental Challenges

- **Multiple interacting coevolving multigraphs involved**
 - **Collaboration multigraph**: who has to collaborate with whom and when.
 - **Communication multigraph**: who has to communicate with whom and when
- **Effects of connectivity topologies:**

Find graph topologies with favorable tradeoff between performance improvement (**benefit**) of collaborative behaviors vs **cost** of collaboration

 - **Small word graphs** achieve such **tradeoff**
 - **Two level algorithm** to provide efficient communication
- Need for **different probability models** – the classical Kolmogorov model is **not correct**
 - Probability models over logics and timed structures
 - Logic of projections in Hilbert spaces – not the Boolean of subsets

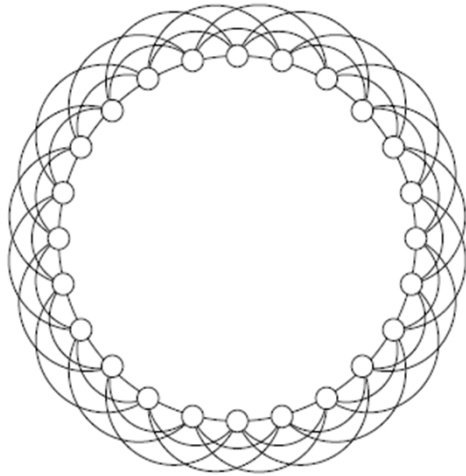
Distributed Algorithms in Networked Systems and Topologies

- Distributed algorithms are essential
 - Agents **communicate with neighbors**, share/process information
 - Agents **perform local** actions
 - **Emergence** of global behaviors
- **Effectiveness** of distributed algorithms
 - The **speed** of convergence
 - **Robustness** to agent/connection failures
 - Energy/ communication **efficiency**
- **Design problem:**

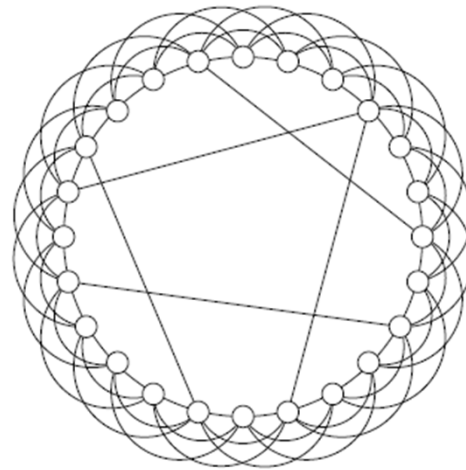
Find graph topologies with favorable tradeoff between performance improvement (**benefit**) vs **cost** of collaboration
- **Example: Small Word graphs** in consensus problems

An Example problem of the Interaction between the Control Graph and the Communication Graph

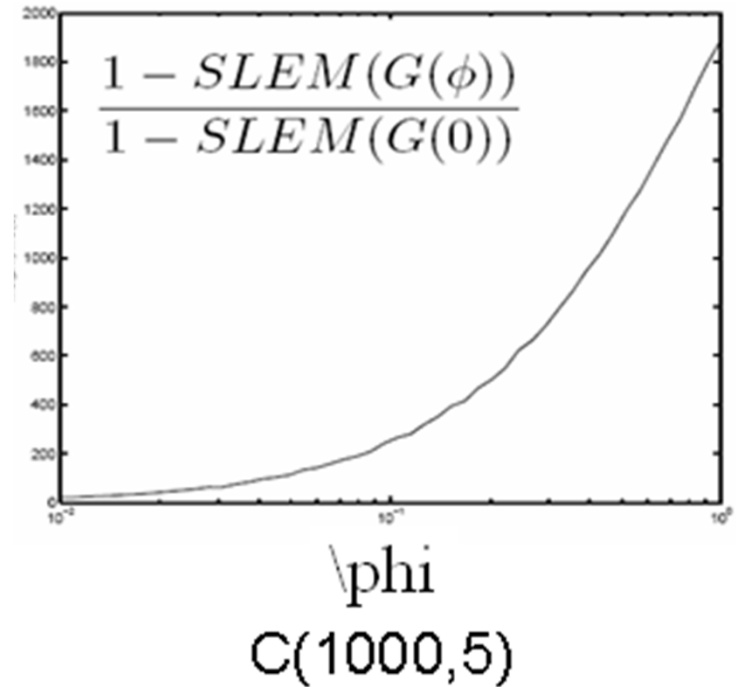
Small World Graphs



Simple Lattice
 $C(n,k)$



Small world: Slight
variation adding $nk\Phi$

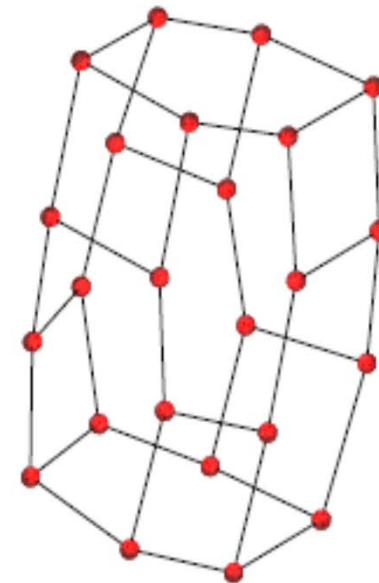
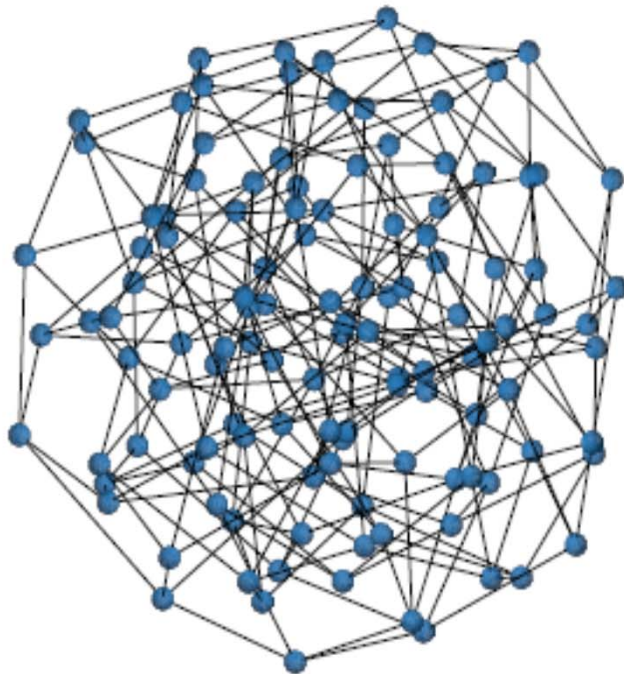


Adding a **small portion** of well-chosen links →
significant increase in convergence rate

Expander Graphs

- First defined by Bassalygo and Pinsker -- 1973
- Fast synchronization of a network of oscillators
- Network where any node is “nearby” any other
- Fast ‘diffusion’ of information in a network
- Fast convergence of consensus
- Decide connectivity with smallest memory
- Random walks converge rapidly
- Easy to construct, even in a distributed way (ZigZag graph product)
- Graph G , **Cheeger constant $h(G)$**
 - All partitions of G to S and S^c ,
 $h(G) = \min (\# \text{edges connecting } S \text{ and } S^c) / (\# \text{nodes in smallest of } S \text{ and } S^c)$
- (k, N, ϵ) **expander** : $h(G) > \epsilon$; **sparse but locally well connected** ($1 - \text{SLEM}(G)$ increases as $h(G)^2$)

Expander Graphs – Ramanujan Graphs

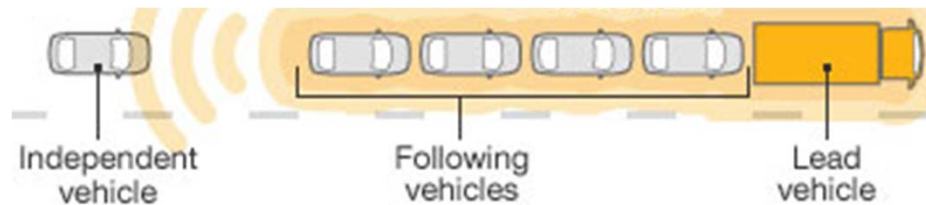


An Example: Vehicle Platooning

Consider an Intelligent Vehicle Highway System (IVHS) where a number of vehicles heading to a common destination form a platoon or a road train.

Advantages-

- improved highway throughput and
- reduced fuel consumption.

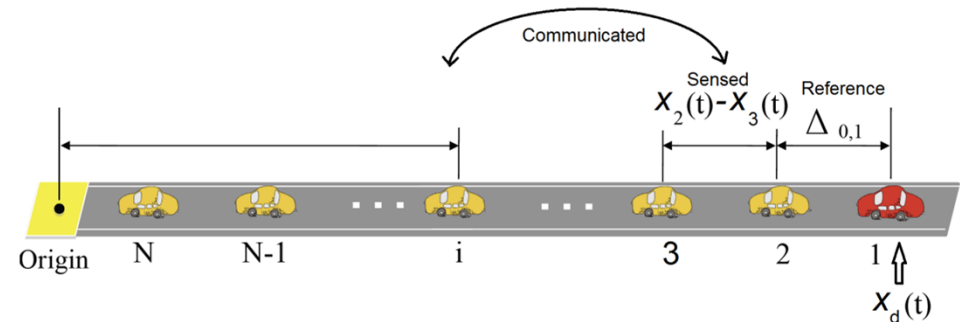


High Speeds, Close Spacing and Multiple Vehicles
➔ Need Automatic Distributed Control

- Vehicles have identical linear dynamics

$$\ddot{x}_i = u_i.$$
- Only lead vehicle is given desired trajectory information $x_d(t)$.
- **Symmetric Control**: i applies a linear feedback law based information available

$$u_i = \frac{1}{deg(i)} \sum_{j \in \mathcal{N}(i)} [-k(x_i - x_j - \Delta_{i,j}) - b(\dot{x}_i - \dot{x}_j)] \\ + \delta(1,i)[-k(x_1 - x_{1,d}) - b(\dot{x}_1 - \dot{x}_{1,d})]$$



Control objective:
Regulation- maintain prescribed reference inter-vehicle spacing.

If the information is restricted to the **nearest neighbor type**, then

- The least damped eigenvalue of the closed loop matrix scales as $O(1/N^2)$
- **String instability** is inevitable- disturbances acting on an individual grow without bounds in the size of the platoon.
- It is **not possible to achieve coherence** or resemblance to a rigid lattice as the formation moves.

Bottom line:
Nearest neighbor type information patterns lead to inadequate control performance.

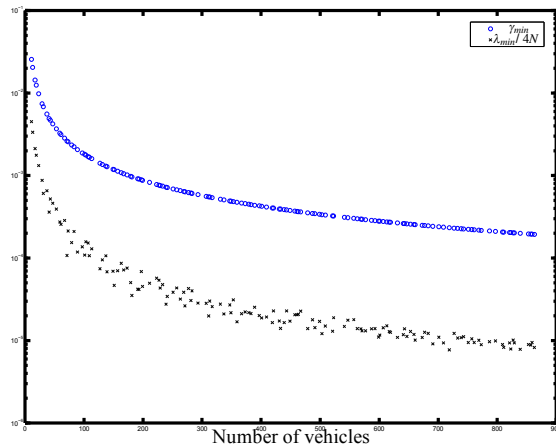
Vehicle Platooning Problem: Better Information Pattern

Information pattern	Communication load $\sim \text{Edges} $	Stability margin
Nearest neighbor type	$O(N)$	$O(1/N^2)$
Complete graph	$O(N^2)$	At most $O(1/N)$

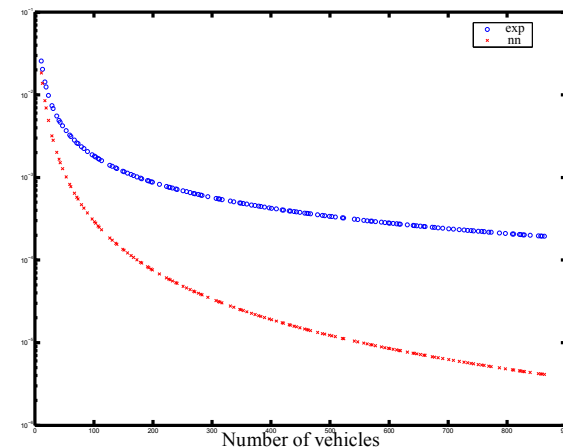
- Is there something in between? Does there exist a “family” of graphs such that one can get improved control performance while limiting the communication load?
- Our result (Menon-Baras 2012-2013):

Expander families	$O(N)$	At most $O(1/N)$
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Some Numerical Simulations and Next Steps



- An experimental verification of the main result stated earlier. The plot of the stability margin γ_{min} is above the lower bound $\frac{\lambda_{min}}{4N}$.



- Experimental verification that expanders outperform nearest neighbor type information patterns. Plot of stability margins with expanders serving as information pattern is above that with nearest neighbor type.

Next steps-

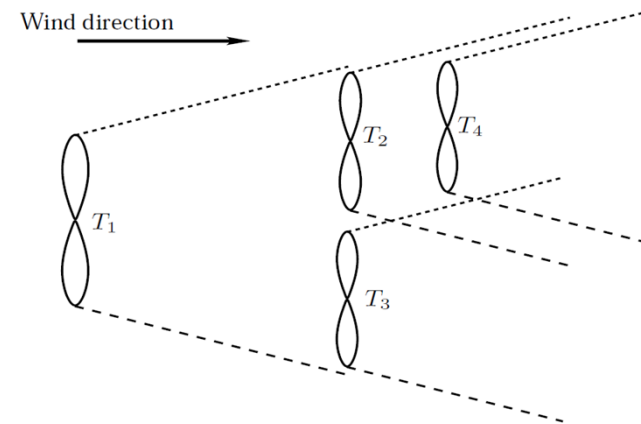
- Investigate the problem under other metrics of control performance like string stability, coherence etc.
- How to synthesize the right expander family?
- More general scenarios for answering the question *“the right information pattern for a given collaborative control task”*.

Interaction Between Control and Communication Graphs: Agents Learn What is Best for the Team

Example: Maximizing Power Production of a Wind Farm



Horns Rev 1. Photographer Christian Steiness



Schematic representation of a wind farm depicting individual turbine wake regions.

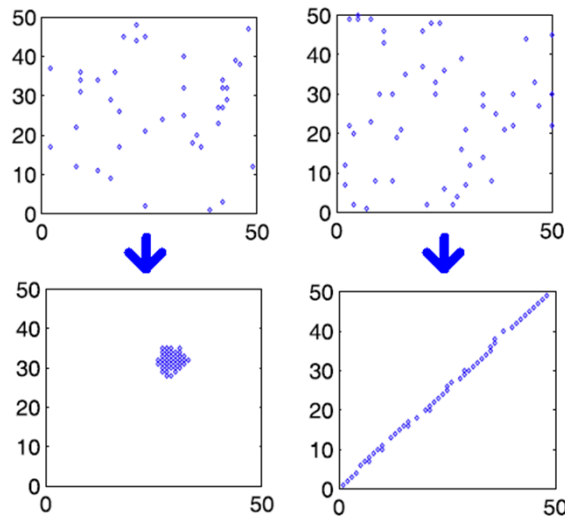
- Aerodynamic interaction between different turbines is not well understood.
- Need on-line decentralized optimization algorithms to maximize total power production.

Assign individual utility

$u_i(t)$ = power produced by turbine i at time t
such that maximizing $\sum_i u_i(t)$ leads to desirable behavior.

Interaction Between Control and Communication Graphs

Example: Formation Control of Robotic Swarms



Simulation results demonstrating rendezvous and gathering along a line^[2]

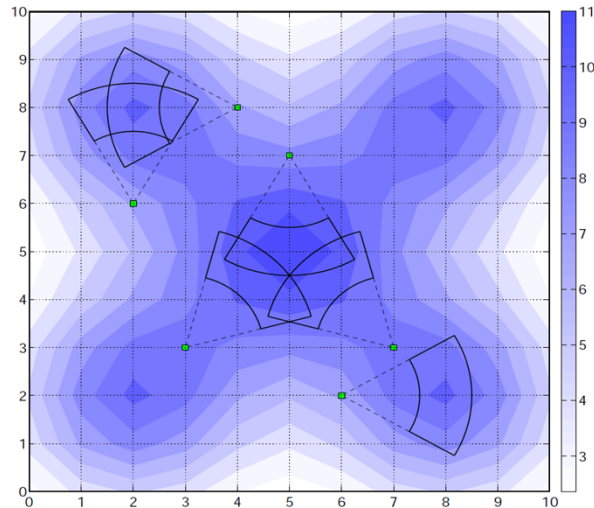
- Deploy a robotic swarm in unknown environment: obstacles, targets etc. have to be discovered.^[3]
- The swarm must form a prescribed geometric formation.
- Robots have limited sensing and communication capabilities.

For rendezvous, design individual utility

$$u_i(s_i) = \frac{1}{|\{s_j \in S: |s_i - s_j| < r\}|} - \alpha \text{dist}_r(s_i, \text{obstacle}),$$

such that minimizing $\sum_i u_i(t)$ leads to desirable behavior.

Example: Mobile Visual Sensor Network Deployment



Darker the shade of blue, more the interest in the site. Sectors represent sensor position and camera viewing angle.

- We wish to monitor events in different sites of varying interest levels.
- All robots monitoring a small set of high interest sites is undesirable w.r.t. coverage.
- Cost associated with information processing.
- How to deploy so “effective coverage” is ensured at “reasonable cost”.

Design individual utility

$$u_i(s, c) = \sum_{s' \in NB(s, c)} \frac{q(s')}{n(s')} - f_i(c),$$

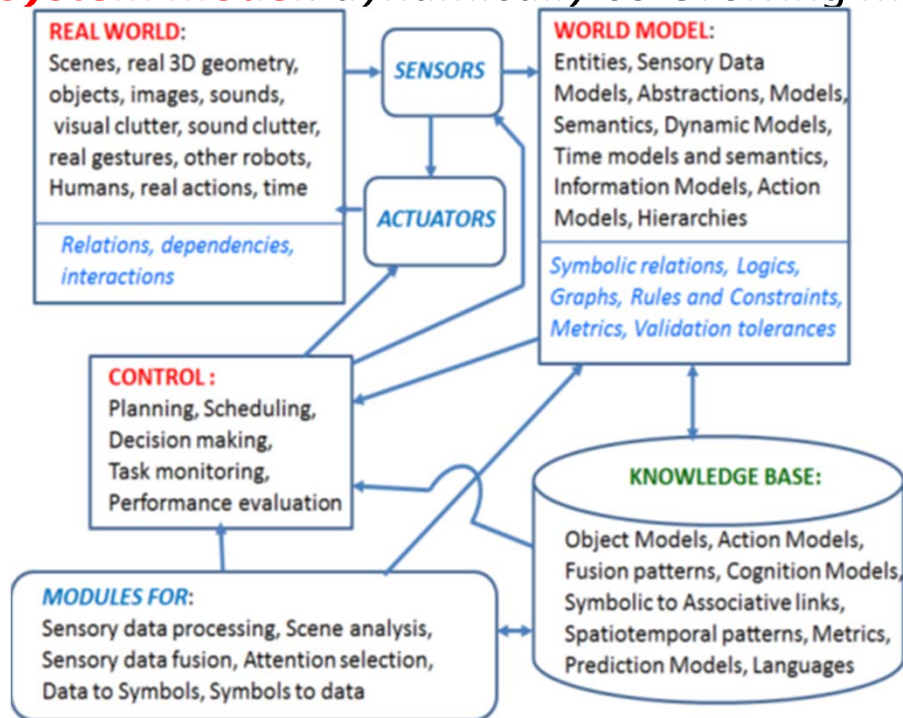
such that maximizing $\sum_i u_i(t)$ leads to desirable behavior.

(here $q(s)$ = interest in observing s , $n(s)$ = number of agents observing s , $NB(s, c)$ = subset of S observable from s when camera viewing angle = c , and $f_i(c)$ = processing cost when the camera viewing angle is c .)

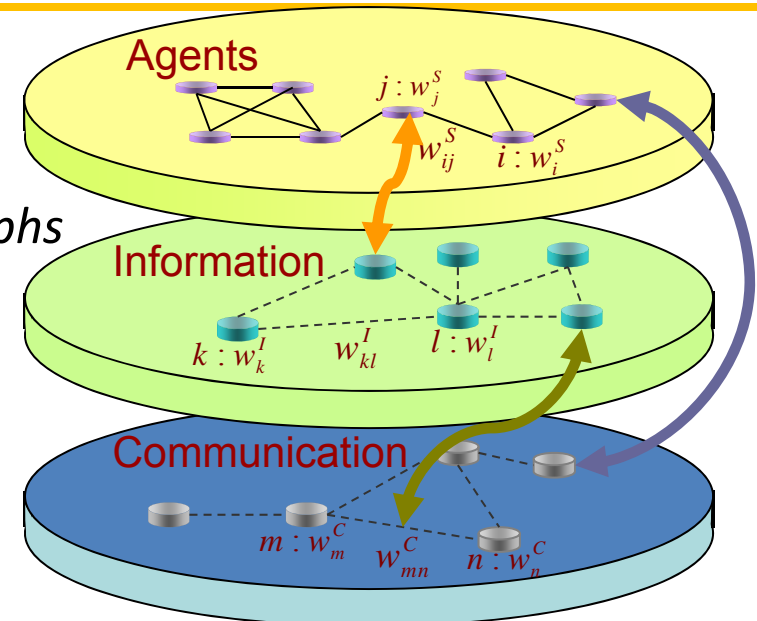
Net-CPS and Collaborative Autonomy

Collaborating agents architecture

- *Nodes and links annotated by weights* or rules
- Annotations are associated across layers,
- **System model**: dynamically co-evolving multigraphs



Each node carries this real vs world model framework



Task-driven integration of perception, control, language

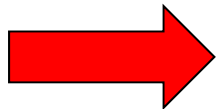
- *Cognitive dialogue*
- *Dynamic attention mechanism*
- *Manipulation grammar*
- *Three-layer architecture*

A Network is ...

- A collection of nodes, agents, ...
that **collaborate** to accomplish actions,
gains, ...
that cannot be accomplished without such
collaboration
- Most significant concept for **dynamic
autonomic networks**

- The nodes **gain** from collaborating
- But collaboration has **costs** (e.g. **communications**)
- Trade-off: **gain** from collaboration vs **cost** of collaboration

Vector metrics involved typically



Constrained Coalitional Games

- **Example 1: Network Formation** -- Effects on Topology
- **Example 2: Collaborative robotics, communications**
- **Example 3: Web-based social networks and services**
- **Example 4: Groups of cancer tumor or virus cells**

• • •

- Users gain by joining a coalition.

- **Wireless networks**

- The benefit of nodes in wireless networks can be the rate of data flow they receive, which is a function of the received power

$$B_{ij} = f(P_j l(d_{ij}))$$

P_j is the power to generate the transmission and $l(d_{ij}) < 1$ is the loss factor

e.g: $B_{ij} = \log(1 + (P_j l(d_{ij}) / N_0))$

- **Social connection** model (Jackson & Wolinsky 1996)

$$B_{ij} = \sum_{j \in g} V \delta^{r_{ij}-1} \quad \text{or} \quad w_i(G)$$

- r_{ij} is # of hops in the shortest path between i and j
- $0 \leq \delta \leq 1$ is the connection gain depreciation rate

- Activating links is costly. $c_i(G) = \sum_{j \in N_i^t} C_{ij}$
 - **Wireless networks**
 - **Energy consumption** for sending data: $C_{ij} = RSd_{ij}^\alpha$
 RS depends on transmitter/receiver antenna gains and system loss not related to propagation
 α : path loss exponent
 - **Data loss** during transmission
 v_i is the environment noise and I_{ij} is the interference

$$C_{ij} = h(v_i, I_{ij}) > 0$$
 - **Social connection model**
 - The more a node is **trusted**, the lower the cost to establish link
e.g. suppose that the trust i has on j is s_{ij} (between 0 and 1),
we can define the cost as the inverse of the trust values

$$C_{ij} = 1 / s_{ij}$$

Pairwise Game and Convergence

- Payoff of node i from the network G is defined as

$$v_i(G) = \text{gain} - \text{cost} = w_i(G) - c_i(G)$$

- Iterated process
 - Node pair ij is selected with probability p_{ij}
 - If link ij is already in the network, the decision is whether to sever it, and otherwise the decision is whether to activate the link
 - The nodes act **myopically**, activating the link if it makes each at least as well off and one strictly better off, and deleting the link if it makes either player better off
 - **End**: if after some time, no additional links are formed or severed
 - **With random mutations**, the game converges to a unique Pareto equilibrium (underlying Markov chain states)

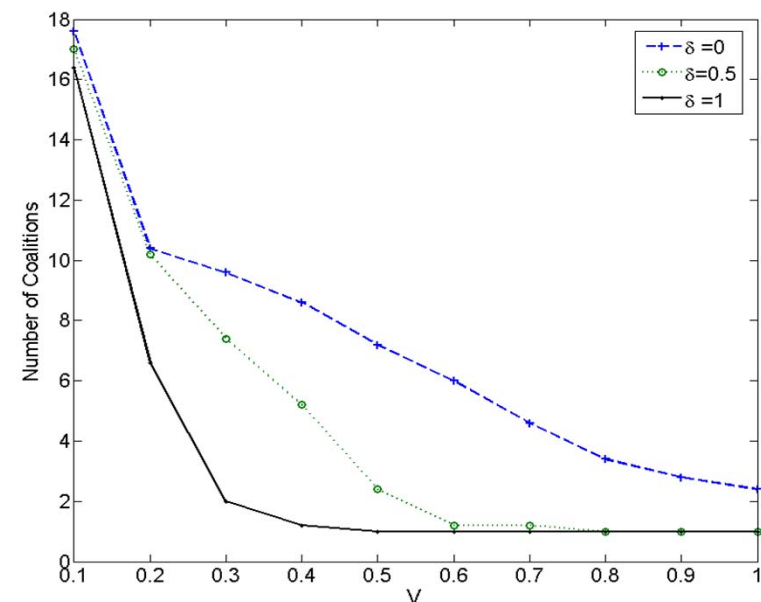
Coalition Formation at the Stable State

- The cost depends on the physical locations of nodes
 - Random network where nodes are placed according to a uniform Poisson point process on the $[0,1] \times [0,1]$ square.
- Theorem:** The coalition formation at the stable state for $n \rightarrow \infty$

— Given $\delta = 0$, $V = P \left(\frac{\ln n}{n} \right)^{\frac{\alpha}{2}}$ is a

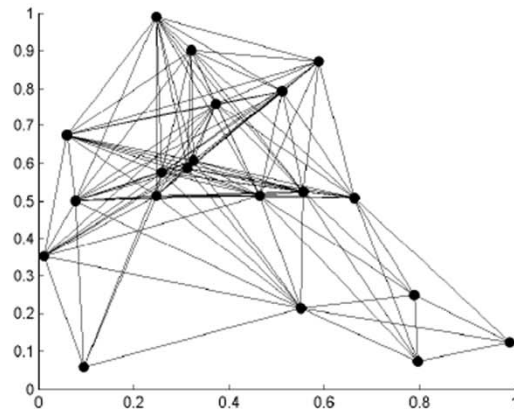
sharp threshold for establishing the grand coalition (number of coalitions = 1).

— For $0 < \delta \leq 1$, the threshold is less than $P \left(\frac{\ln n}{n} \right)^{\frac{\alpha}{2}}$.

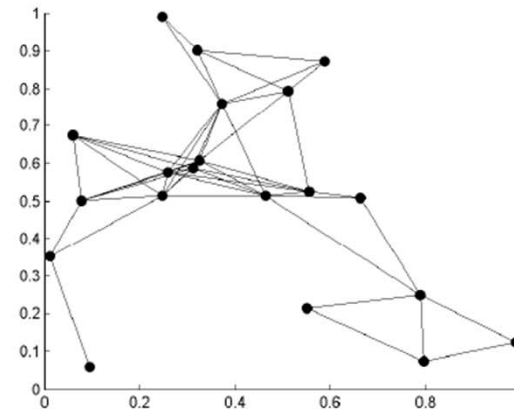


$n = 20$

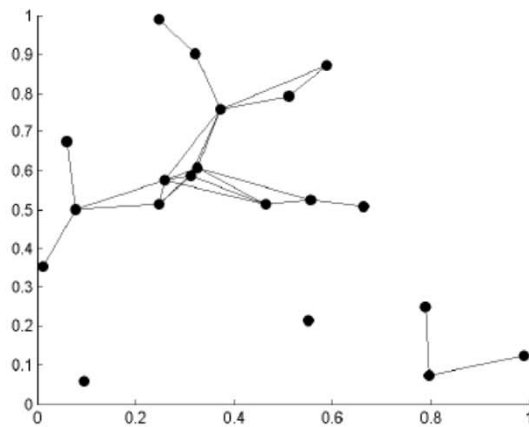
Topologies Formed



(a) $P = 0.5$ (low cost); complete graph



(b) $P = 2$ (middle cost); small world topology



(c) $P = 4$ (high cost); partitioned network

Trust as Mechanism to Induce Collaboration

- Trust **is an incentive** for collaboration (Arrow 1974)
 - Nodes who refrain from cooperation get lower trust values
 - Eventually penalized because **other nodes tend to only cooperate with highly trusted ones**.
- For node i **loss for not cooperating** with node j is a nondecreasing function of J_{ji} , $f(J_{ji})$,
- New characteristic function is

$$\nu(\mathcal{S}) = \sum_{i,j \in \mathcal{S}} J_{ij} - \sum_{i \in \mathcal{S}, j \notin \mathcal{S}} f(J_{ij})$$

(Baras-Jiang 04, 05)

- **Theorem:** if $\forall i, j, J_{ij} + f(J_{ji}) \geq 0$, the core is nonempty and $x_i = \sum_{j \in N_i} J_{ij}$ is a feasible payoff allocation in the core.

By introducing a trust mechanism, all nodes are induced to collaborate without any negotiation

Dynamic Coalition Formation

Two linked dynamics

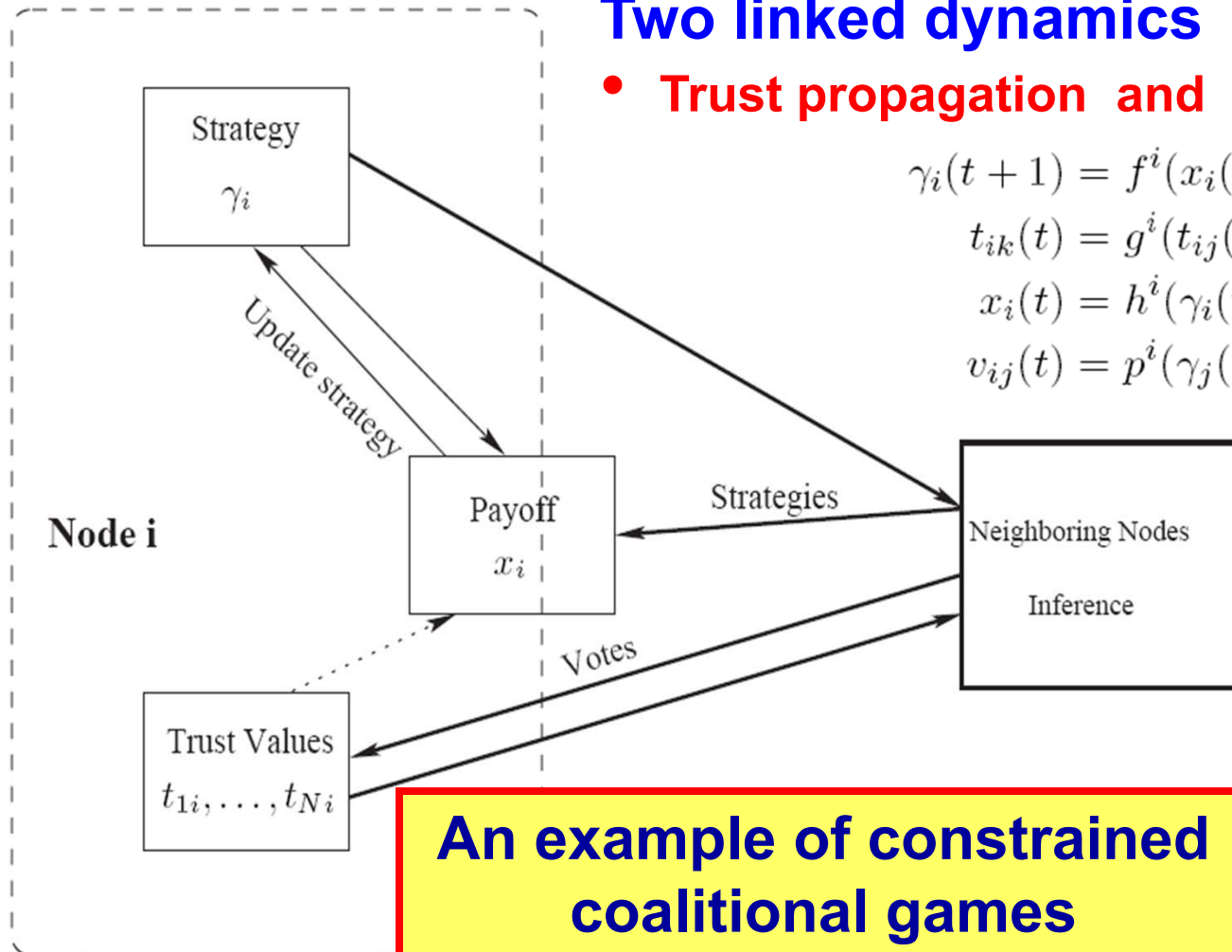
- Trust propagation and Game evolution

$$\gamma_i(t+1) = f^i(x_i(t), \gamma_i(t), \gamma_j(t), t_{ij}(t))$$

$$t_{ik}(t) = g^i(t_{ij}(t), v_{jk}(t)) \quad \forall k \in N$$

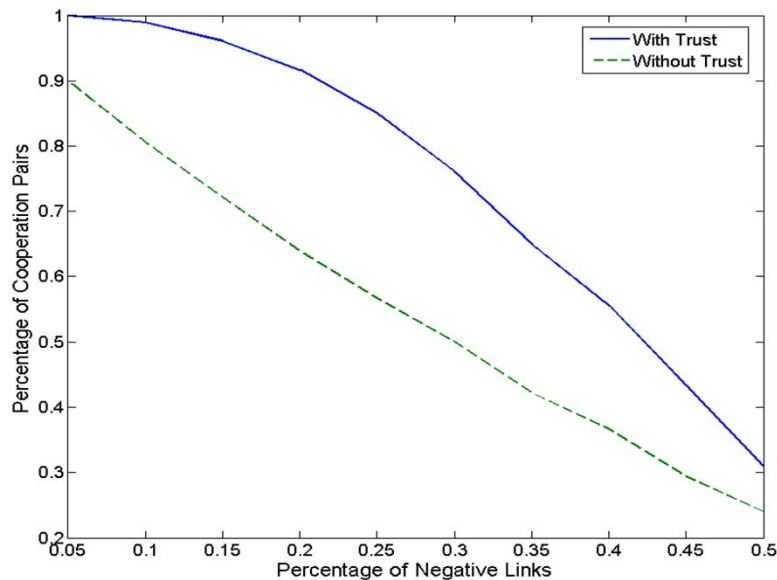
$$x_i(t) = h^i(\gamma_i(t), \gamma_j(t))$$

$$v_{ij}(t) = p^i(\gamma_j(t), t_{ji}(t))$$

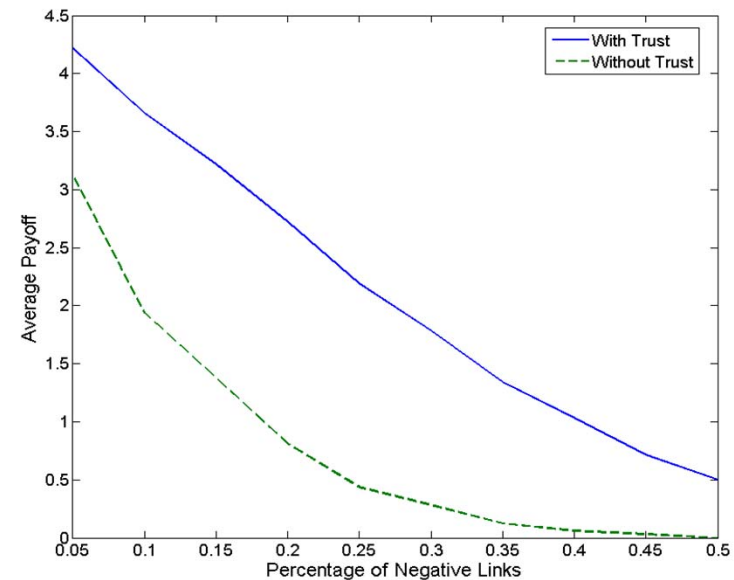


Stability of
dynamic
coalition
Nash equilibrium

- Theorem:** $\forall i \in N_i$ and $x_i = \sum_{j \in N_i} J_{ij}$, there exists τ_0 , such that for a reestablishing period $\tau > \tau_0$ (Baras-Jiang 05, 09, 10)
 - iterated game converges to Nash equilibrium;
 - In the Nash equilibrium, all nodes cooperate with all their neighbors.
- Compare games **with** (**without**) trust mechanism, strategy update:



Percentage of cooperating pairs vs negative links



Average payoffs vs negative links

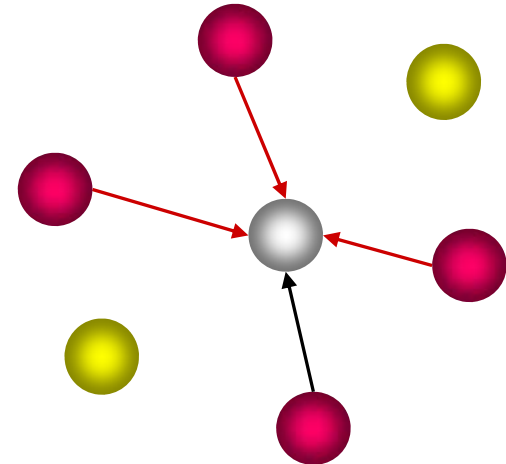
Trust Evaluation: Local Voting Rule

- In **homogenous** networks, the trustworthiness of an agent is based on other peers' opinion
 - The most straightforward scheme is to ask neighbors to “**vote**” for it
 - Values of the votes are equal to c_{ij}

- Iterative voting rule:

$$s_i(k+1) = f\left(J_{ji}s_j(k) \mid j \in N_i\right)$$

- Evaluation starts from a small set of trusted nodes
- Our interest is to study **evolution** of the estimated trust value s_i and its property at the **equilibrium**



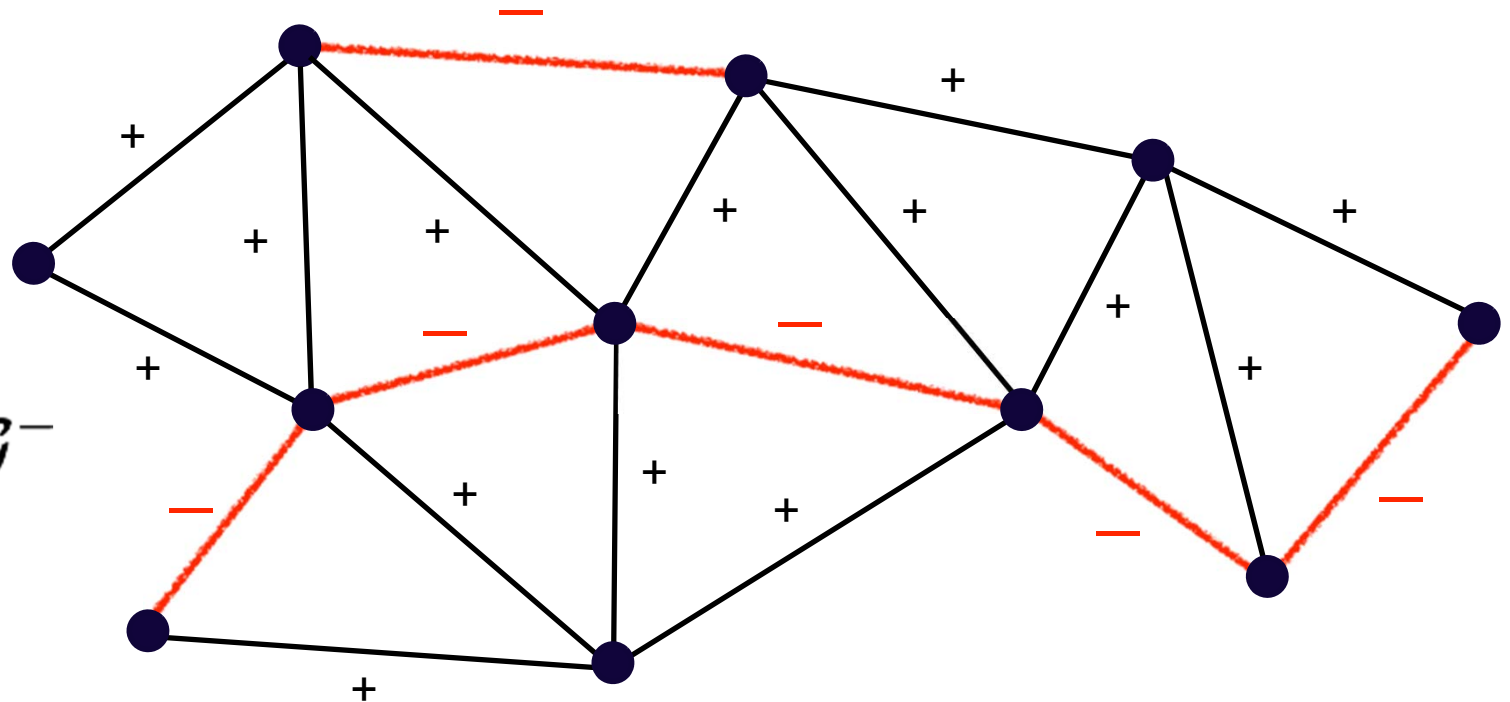
More Generally: Node Dynamics

$$x_i(k+1) = f_i\left(x_i(k); x_j(k), j \in \mathcal{N}_i\right)$$

- Engineered control and algorithms for collective tasks such as optimization, formation, coverage, estimation, and filtering.
- Social and biological modeling to peer behavior in a society or in a group.

Nodes are cooperative and rational!

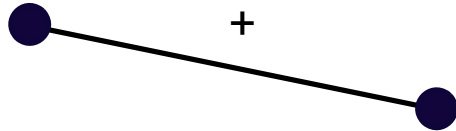
But are they?



$$\mathcal{G} = \mathcal{G}^+ \cup \mathcal{G}^-$$

- Fixed
- Undirected
- Deterministic
- Connected

$$\mathcal{N}_i = \mathcal{N}_i^+ \cup \mathcal{N}_i^-$$



$$x_i(k+1) = x_i(k) + \alpha(x_j(k) - x_i(k))$$

- Classical DeGroot's rule for opinion update between two trustful individuals in a social network.
- Foundation of many distributed engineering solutions e.g., Jadbabaie et al. 2003, Nedich et al. 2009, Kar and Moura 2013, etc.

Negative Dynamics



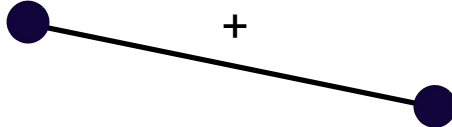
- State-Flipping Model (Altafini 2013 TAC)

$$x_i(k+1) = x_i(k) + \beta(-x_j(k) - x_i(k))$$

- Relative-State-Flipping Model (Shi et al. 2013 JSAC)

$$x_i(k+1) = x_i(k) + \beta(x_i(k) - x_j(k))$$

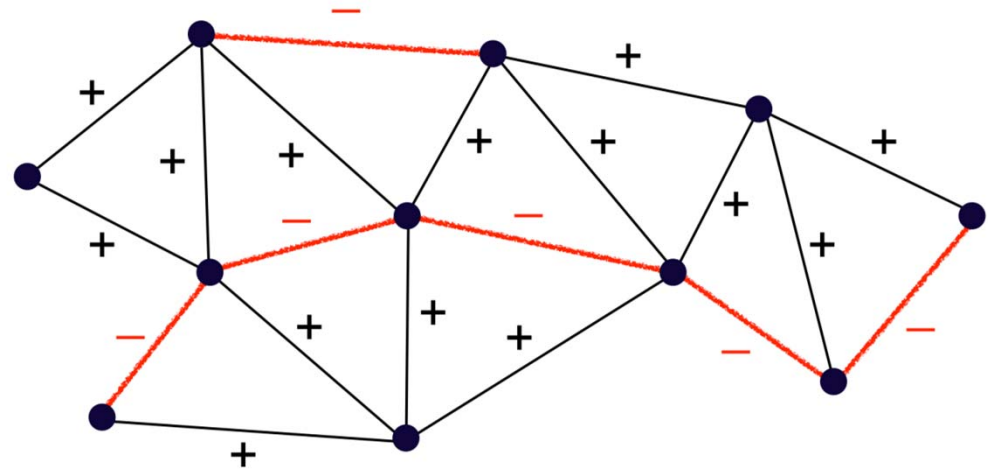
State-Flipping Model



$$x_i(k+1) = x_i(k) + \alpha(x_j(k) - x_i(k))$$



$$x_i(k+1) = x_i(k) + \beta(-x_j(k) - x_i(k))$$



Lemma. Let $\alpha|\mathcal{N}_i^+| + \beta|\mathcal{N}_i^-| < 1$ for all i . For any initial value \mathbf{x}_0 , there exists $\mathbf{y}(\mathbf{x}_0)$ with $\mathbf{A}\mathbf{y} = \mathbf{y}$ such that

$$\lim_{k \rightarrow \infty} x_i(k) = y_i, \quad i = 1, \dots, N.$$

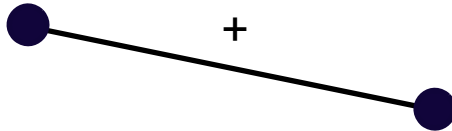
Theorem. (i) If \mathcal{G} is strongly balanced, then there is a partition of the node set \mathcal{V} into \mathcal{V}_1 and \mathcal{V}_2 such that

$$\begin{aligned} y_i &= y_*, & i \in \mathcal{V}_1; \\ y_i &= -y_*, & i \in \mathcal{V}_2. \end{aligned}$$

(ii) If \mathcal{G} is not strongly balanced, then $y_i = 0$ for all i .

A signed graph is **strongly balanced** if the node set can be divided into two disjoint subsets such that negative links can only exist between them; **weakly balanced** if such a partition contains maybe more than two subsets.

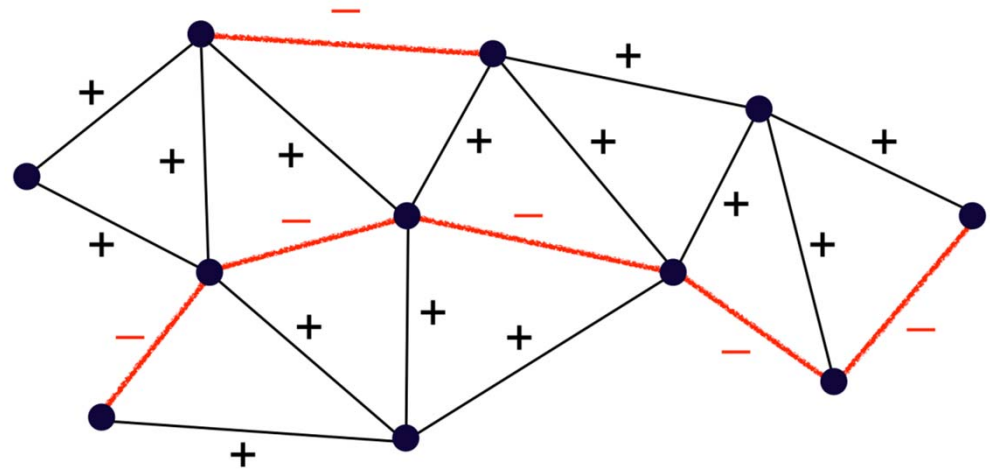
Relative-State-Flipping Model



$$x_i(k+1) = x_i(k) + \alpha(x_j(k) - x_i(k))$$



$$x_i(k+1) = x_i(k) + \beta(x_i(k) - x_j(k))$$



Theorem. Suppose \mathcal{G}^+ is connected and \mathcal{G}^- is non-empty. Let $\alpha|\mathcal{N}_i^+| < 1$. Then there exists β_* such that

(i) if $\beta < \beta_*$,

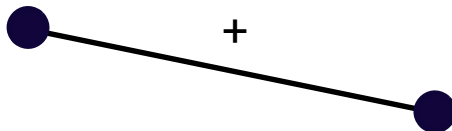
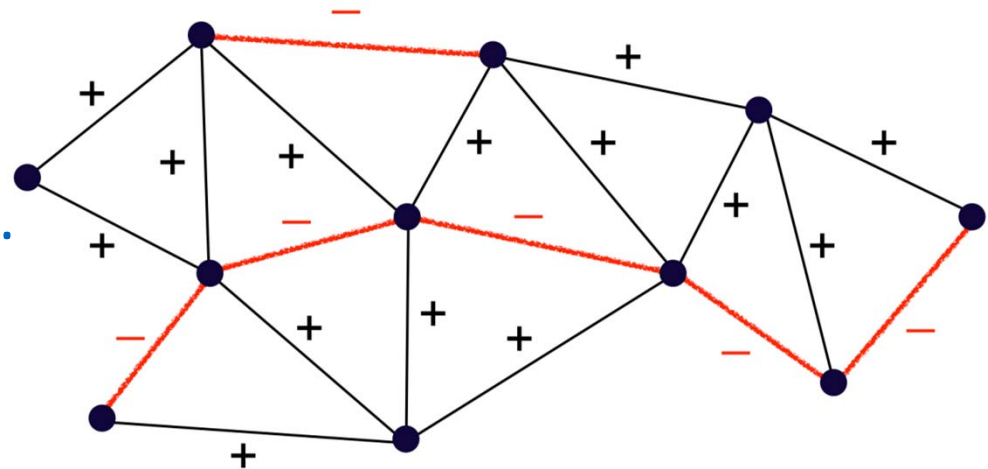
$$\lim_{k \rightarrow \infty} x_i(k) = \frac{\sum_{j=1}^N x_j(0)}{N}, i = 1, \dots, N;$$

(ii) if $\beta > \beta_*$,

$$\lim_{k \rightarrow \infty} \|\mathbf{x}(k)\| = \infty$$

for some initial values.

A pair (i,j) is randomly selected.
The two selected nodes update.



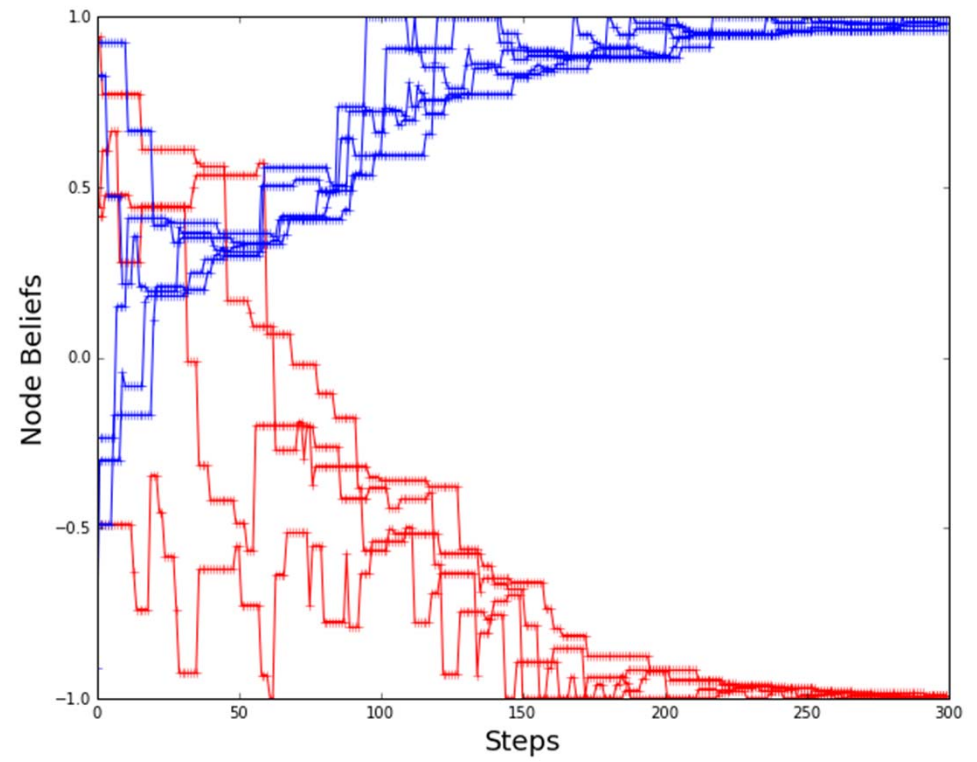
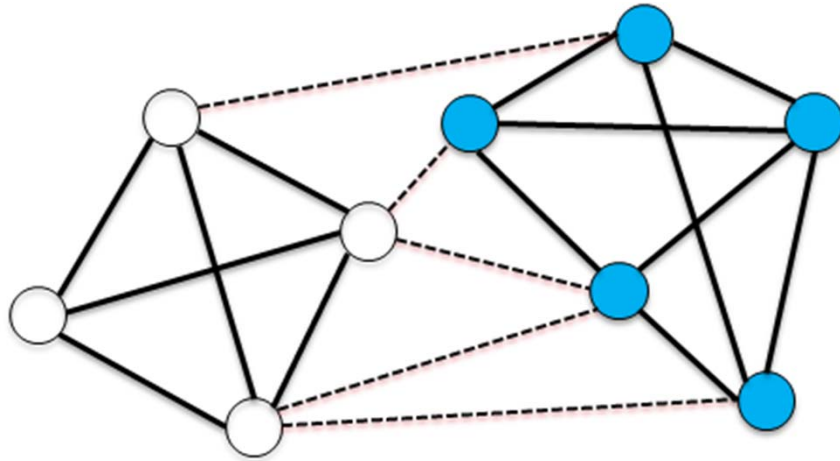
$$x_i(k+1) = x_i(k) + \alpha(x_j(k) - x_i(k))$$



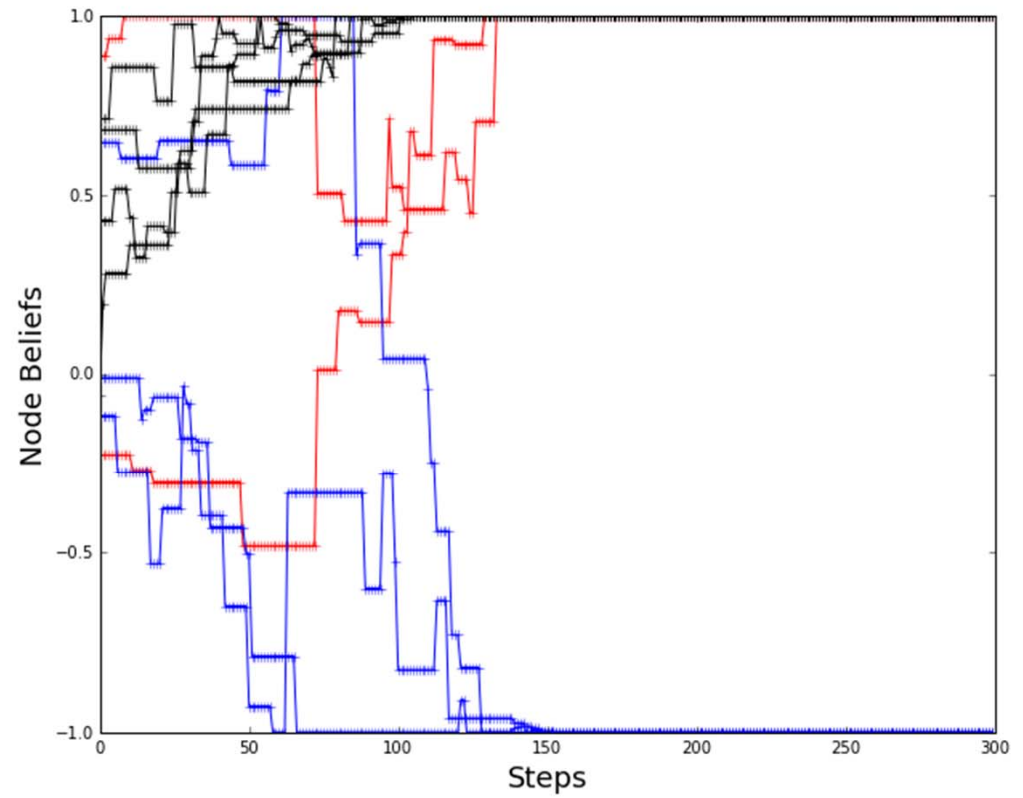
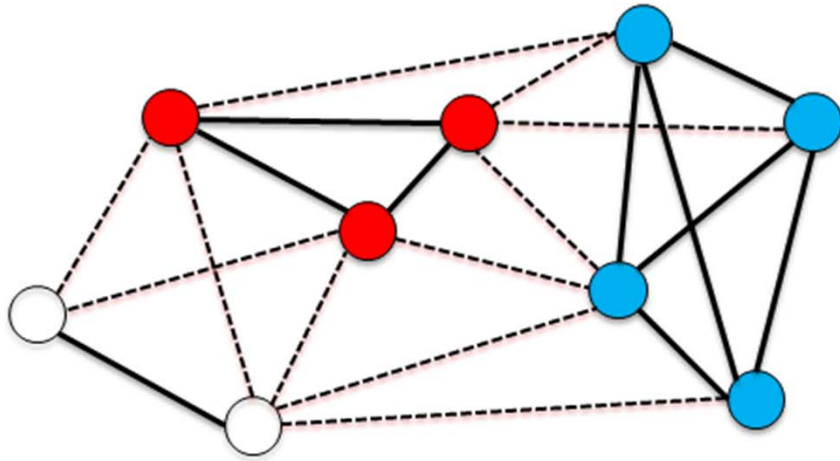
S-F Model $x_i(k+1) = x_i(k) + \beta(-x_j(k) - x_i(k))$

R-S-F Model $x_i(k+1) = x_i(k) + \beta(x_i(k) - x_j(k))$

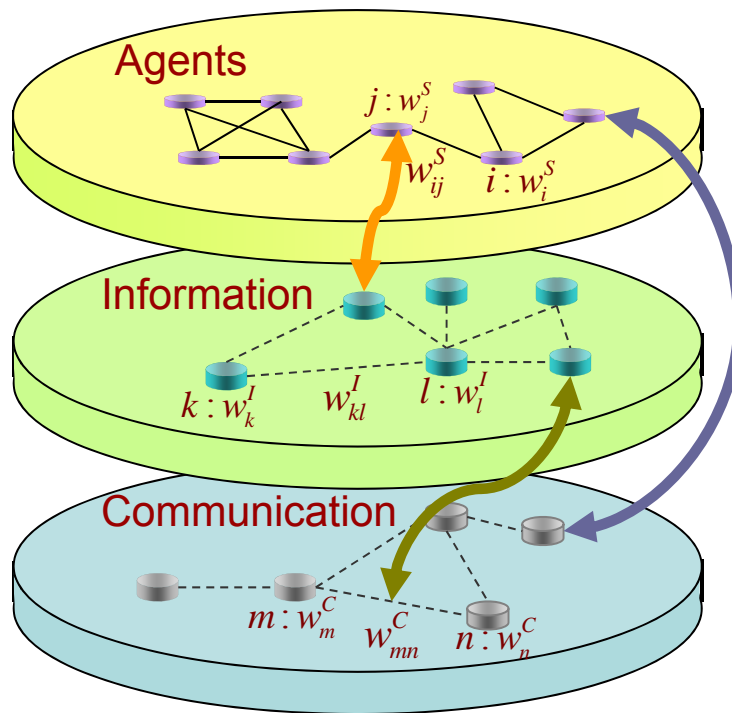
Relative-State-Flipping Model



Relative-State-Flipping Model



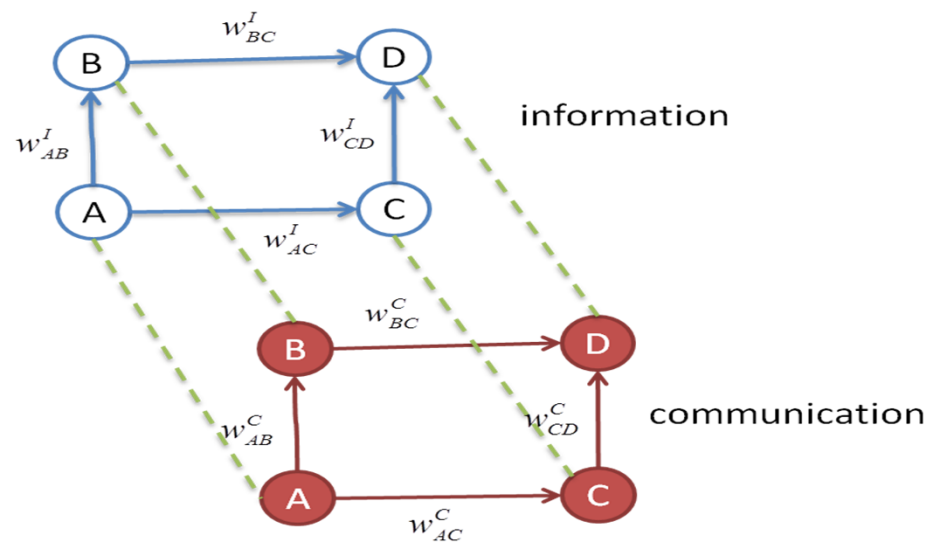
Composite Trust: Value Directed Graphs



- Value directed multi-graphs with weighted nodes
 - Inspired by advanced dynamic network models and trust research in social networks
 - Directed graphs with weights on their links and nodes
 - Weights represent trust metrics on both links and nodes

Example

- A two-level graphs with trust weights



- Information semiring is $\langle W^I, \max, \min, 0, 1 \rangle$
- Communication semiring is $\langle W^C, \max, \min, 0, 1 \rangle$
- Trust semiring is $TS = \langle W^I \times W^C, +_{\text{trust}}, \times_{\text{trust}}, 0, 1 \rangle$

Example (cont.)

- Two different set of constraint preferences
 - Information preferred

$$(w_1^I, w_1^C) +_{trust} (w_2^I, w_2^C) = \begin{cases} (w_1^I, w_1^C) & \text{if } w_1^I > w_2^I \\ (w_2^I, w_2^C) & \text{if } w_1^I < w_2^I \\ (w_1^I, \max(w_1^C, w_2^C)) & \text{if } w_1^I = w_2^I \end{cases}$$

$$(w_1^I, w_1^C) \times_{trust} (w_2^I, w_2^C) = (\min(w_1^I, w_2^I), \min(w_1^C, w_2^C))$$

- Communication preferred

$$(w_1^I, w_1^C) +_{trust} (w_2^I, w_2^C) = \begin{cases} (w_1^I, w_1^C) & \text{if } w_1^C > w_2^C \\ (w_2^I, w_2^C) & \text{if } w_1^C < w_2^C \\ (\max(w_1^I, w_2^I), w_1^C) & \text{if } w_1^C = w_2^C \end{cases}$$

$$(w_1^I, w_1^C) \times_{trust} (w_2^I, w_2^C) = (\min(w_1^I, w_2^I), \min(w_1^C, w_2^C))$$

Example (cont.)

- This specific trust SCSP has a distributed solution where the following algorithm is carried out at every node in the network

Algorithm: The distributed solution to solve the SCSP.

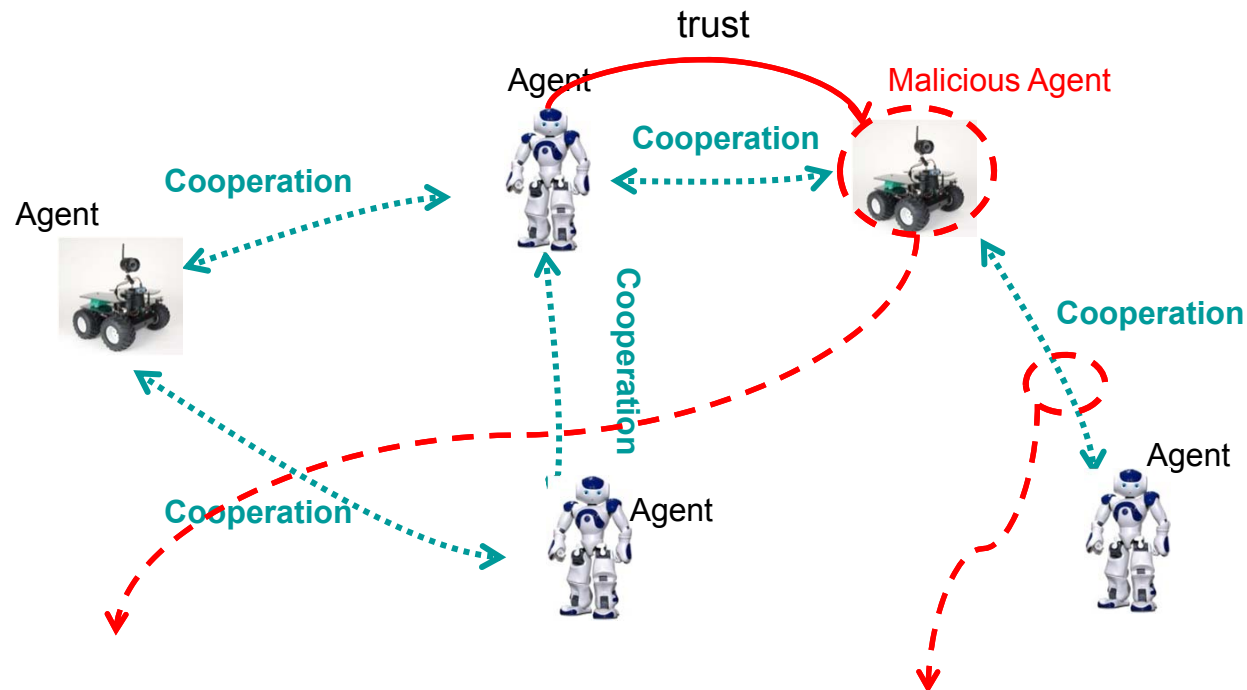
Repeat

$$X_k^{n+1}(D) = \sum_{l \in N_k} w_{kl} \times_{trust} X_l^n(D)$$

Until $X_k^n(D)$ converges.

- $X_l^n(D)$ represents the evaluated trust to target D via a chain of n direct trust relations
- $\sum = \times_{trust}$

- Solve the problem via detecting adversaries in networks of low connectivity.
- We integrate a **trust evaluation mechanism** into our consensus algorithm, and propose a two-layer hierarchical framework.
 - Trust is established via **headers (aka trusted nodes)**
 - The top layer is a super-step running a **vectorized consensus algorithm**
 - The bottom layer is a sub-step executing our **parallel vectorized voting scheme**.
 - Information is exchanged between the two layers – they **collaborate**
- We demonstrate via examples solvable by our approach but not otherwise
- We also derive an upper bound on the number of adversaries that our algorithm can resist in each super-step



Malicious agent:

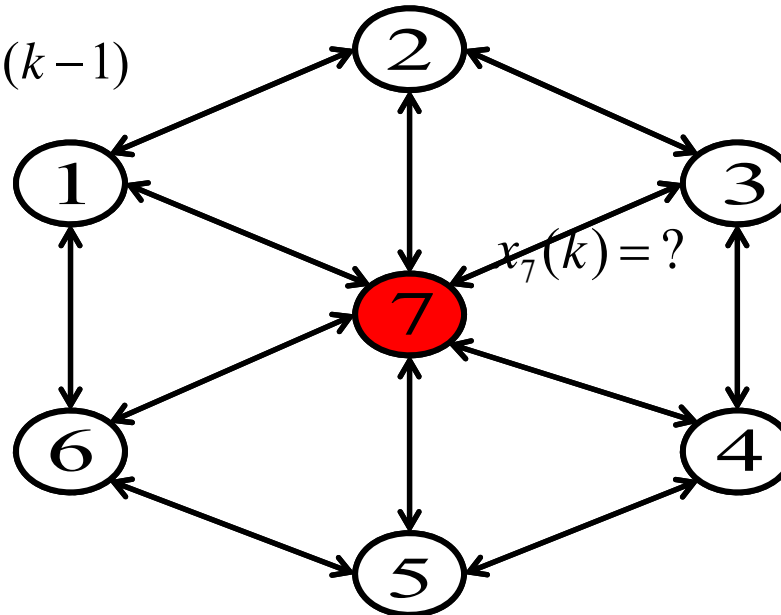
- Multiparty secure computation
[4] Garay, Juan A., and Rafail Ostrovsky. "Almost-everywhere secure computation." Advances in Cryptology–EUROCRYPT 2008.
- Consensus with Byzantine adversaries (System theory)
[5] Pasqualetti, Fabio, Antonio Bicchi, and Francesco Bullo. "Consensus computation in unreliable networks: A system theoretic approach," IEEE TAC, 2012.

Link Jam & Noise Injection:

- [3] Khanafer, Ali, Behrouz Touri, and Tamer Basar. "Consensus in the presence of an adversary." 3rd IFAC Workshop on Distributed Estimation and Control in Networked Systems (NecSys). 2012.

Problem Formulation – Simple Example

$$x_1(k) = \sum_{j \in N_1} w_{1j} x_j(k-1)$$



Goal:

Detect malicious nodes and isolate them from consensus algorithm.

- Without considering failures, for certain nodes, the consensus problem in distributed control can be solved by simply iteratively calculating weighted averages of nodes' neighboring states.
 - Network of agents modeled by directed graph $G(k) = (V; E(k))$
 V denotes the set of nodes and $E(k)$ the set of edges at time k
 $N_i(k) = \{j \mid e_{ij}(k) \in E(k), j \neq i\}$ set of neighbor nodes of i
 "can hear from at time k ". $N_i^+(k) = N_i(k) \cup \{i\}$
 - Nodes' states (decisions, beliefs, opinions, etc.) evolve in time according to the dynamics:

$$x_i(k) = \sum_{j \in N_i(k)} w_{ij}(k) x_j(k-1) + w_{ii}(k) x_i(k-1)$$

$X(k) = \{x_1(k), x_2(k), \dots, x_N(k)\}^T$ N -dimensional vector of nodes' states at time k .

$W(k)$ is the updating matrix (weight matrix) at time k , rows sum to 1.

- Several different strategies have been proposed to solve the problem of distributed consensus with Byzantine adversaries.
- Related works rely on strong conditions on network topology:

$$c \geq 2f_b + 1$$

$$n \geq 3f_b$$

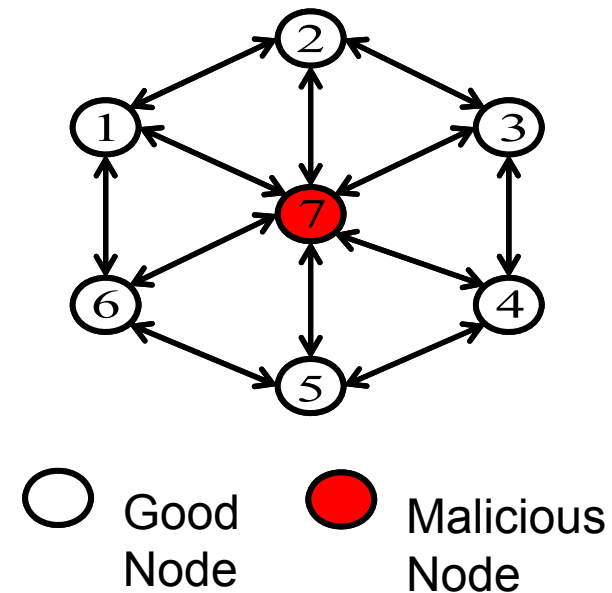
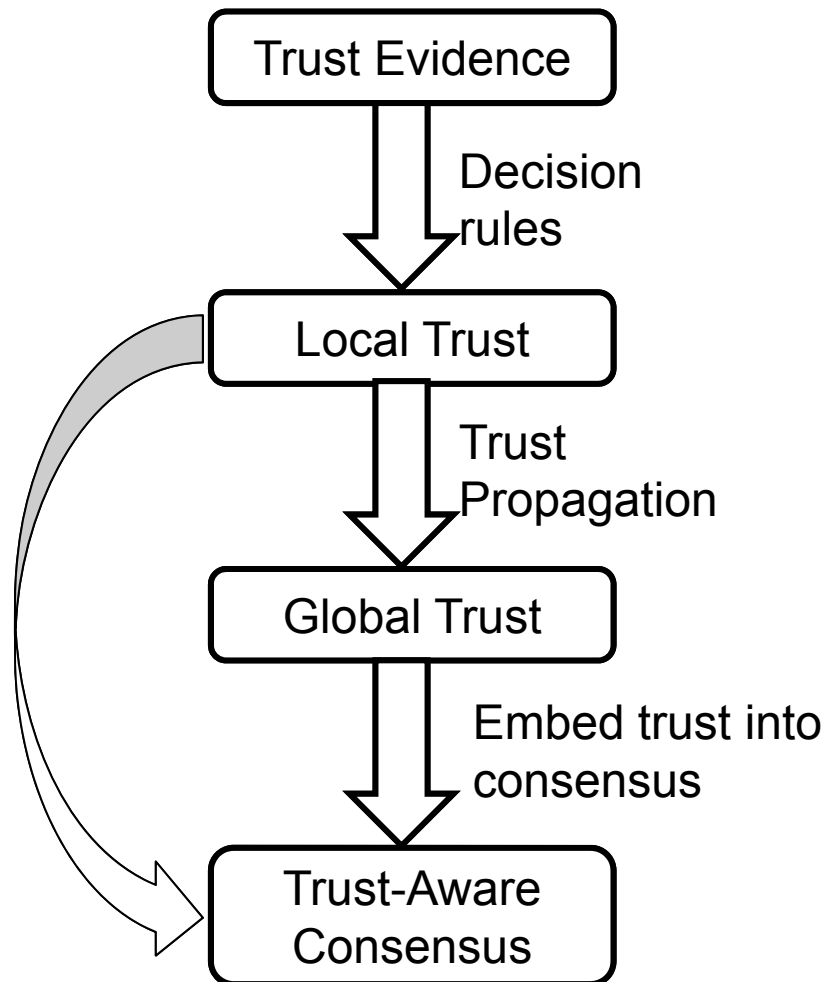
– $c = \min\{c_{ij}, \forall i, j \in V, i \neq j\}$ is the **connectivity of the network**,

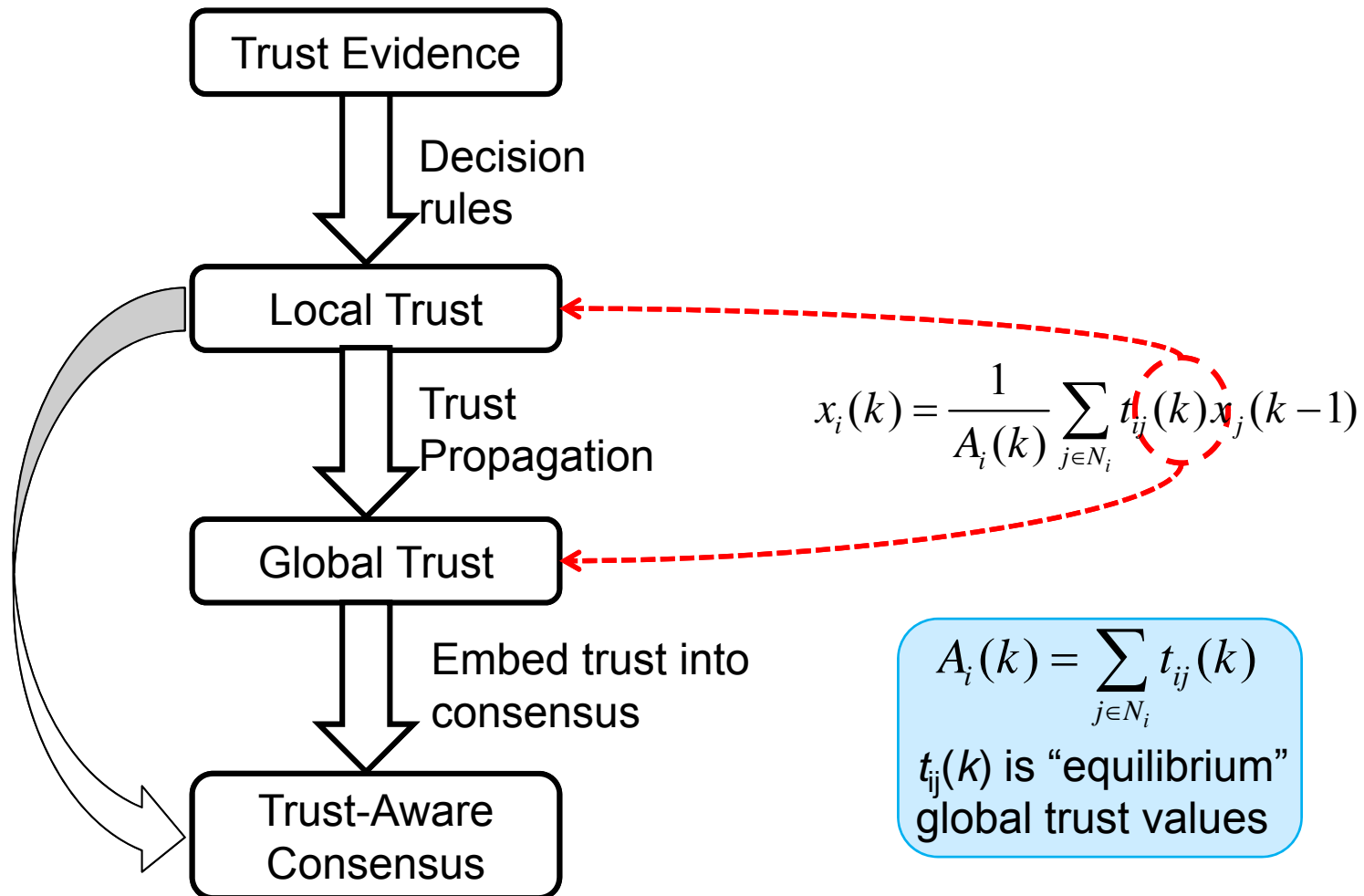
c_{ij} is the number of disjoint paths between node i and node j .

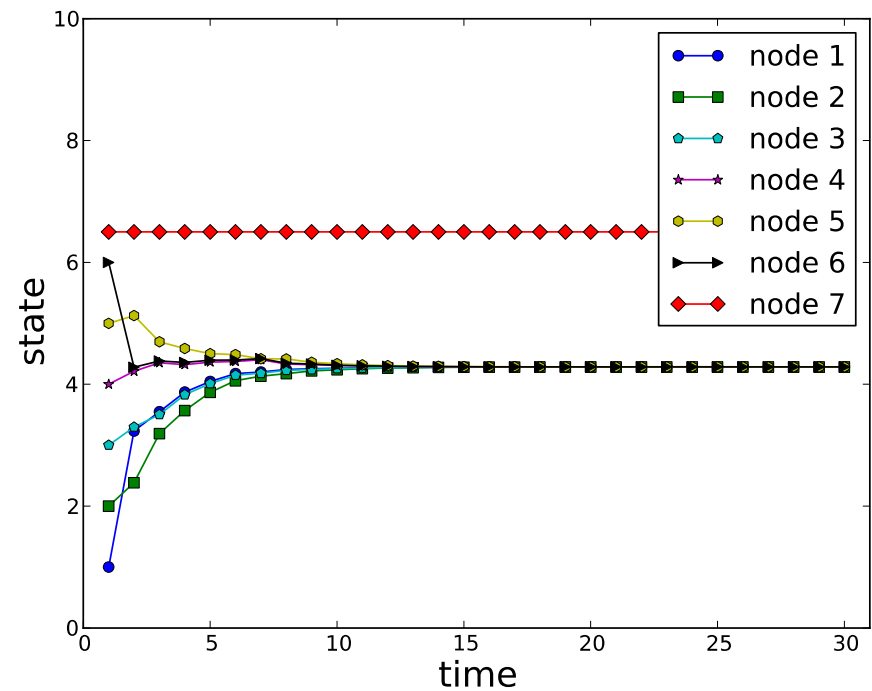
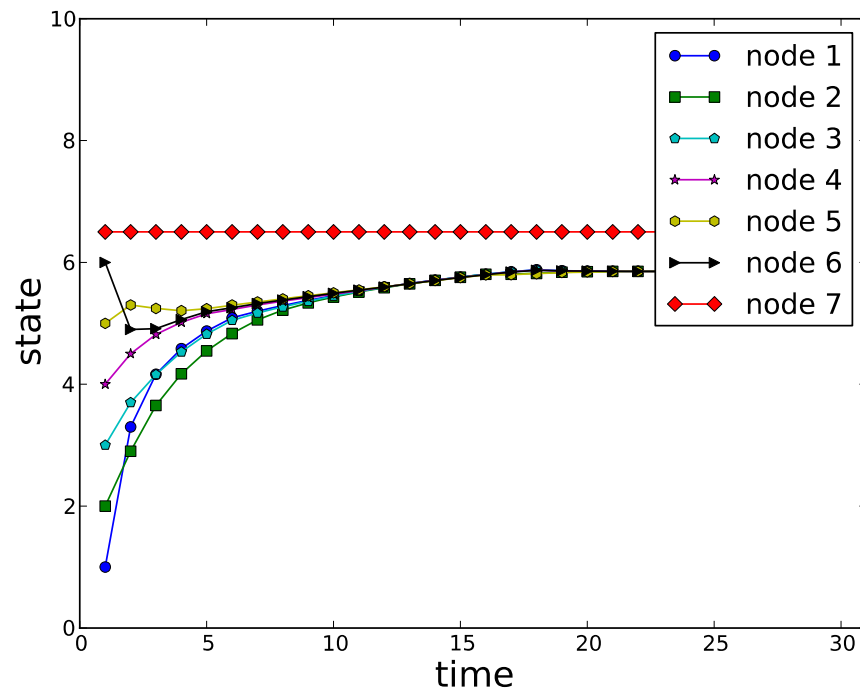
– f_b is the number of Byzantine attackers, n is the number of nodes.

- However, these conditions about network connectivity used in related and past works cannot be verified in many situations.

Trust-Aware Consensus







Adversary outputs constant message. Figure on the left has no trust propagation. Figure on the right has trust propagation.

Networked Systems – Fundamental Problems

- *Interaction between information and control*
 - controllers communicate via “signaling strategies”
 - “information neighborhoods” for controllers
 - cost of information versus cost of control
- There does not exist todate a satisfactory formulation of the joint “optimization” problem in information flow and control
- Important to develop theories that treat control strategies and information patterns in a balanced manner
- *Interactions between measurements by different agents and between system dynamics and measurements*
 - Akin to very strong interaction between information and control
 - Often the case where one cannot prove existence of an optimal control law (or design)

Simpler Problem: Information Retrieval (IR)

- Relevance is subjective – varies from user to user
 - Relevance depends on the state of the user – but it changes as user acquires information
 - Plenty of evidence that relevance of a document to a user **changes as the user interacts with the system**
 - Probabilistic assessment of relevance – **but on what event logic?**
 - **Ample experimental evidence** : IR based on current Boolean model does not deliver required performance (Van Rijsbergen, 2006)
-

Non-commutative Probability Examples

- Tracking and identification of moving objects using multiple-cameras
- High-level activity detection and anomalous activity mining from multiple perspectives
- Trust in social networks
 - Neuropsychological studies, emotional activation, interpersonal relationships, trust, decisions relying on trust.
- Human judgments and noncommutativity
 - Based on indefinite state, create than record, disturb each other, do not obey classic logic, law of total probability does not hold

Non-commutative Probability Examples

- Human cognition and decision making
 - Disjunction effect
 - interference between categorization and decision making
 - Conjunction fallacy
 - Compositionality in the semantics of cognitive information processing
 - Related to question order effects that cannot be explained by classical probability models
- Classical Kolmogorov-like models **cannot explain any of the observed phenomena** and measurements, in examples.
- Recent studies utilizing the alternative quantum-like probabilities and logics have shown considerable agreement with the experimental data in these phenomena

Multi-Agent Networked Systems: Event-State-Operation Structures



- Multi-agent system – **incompatible events** – occurrence cannot be verified by two or more agents
- Manifestation of **communication constraints** – or interactions
 - Sensor networks – domain of observation or sensor range
 - Multi-agent control – domain of influence or control range
- **Incompatible measurements** – new essential concept in multi-agent systems
- Need to build probabilistic models that have incompatibility built-in – Conditioning and its modeling is at the center of this
- Multi-agent setting: data/measurements lead to two incompatible events – how do we describe their conjunction?
- Introduce generalizations of conditional probability and conditional expectation

Conclusions

- Three-layer Net-CPS model
- Effects of topology on distributed algorithm performance
- Fundamental tradeoff between the benefit from collaboration and the cost for collaboration – constrained coalitional games
- Trust as catalyst for collaboration
- Trust and Mistrust dynamics
- New probabilistic models – similar to the quantum mechanical ones
- **For the future:** More on Value of Information, Control -- Information Duality, Complexity and consequences, New Logics and Collaborative Teams, Noncommutative Probability

Thank you!

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Questions?
