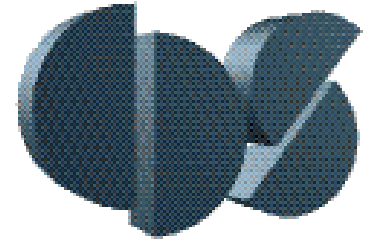




# Feedback and Control in Biological Circuit Design (Synthetic Biology)



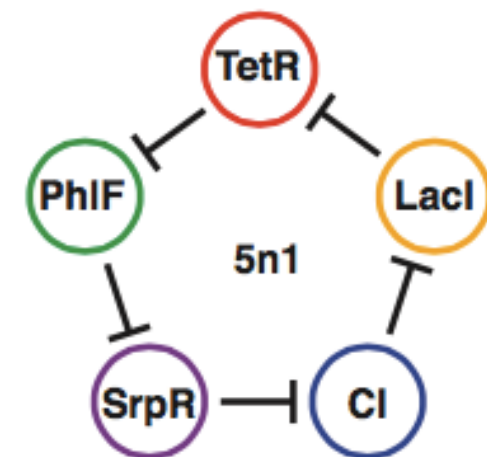
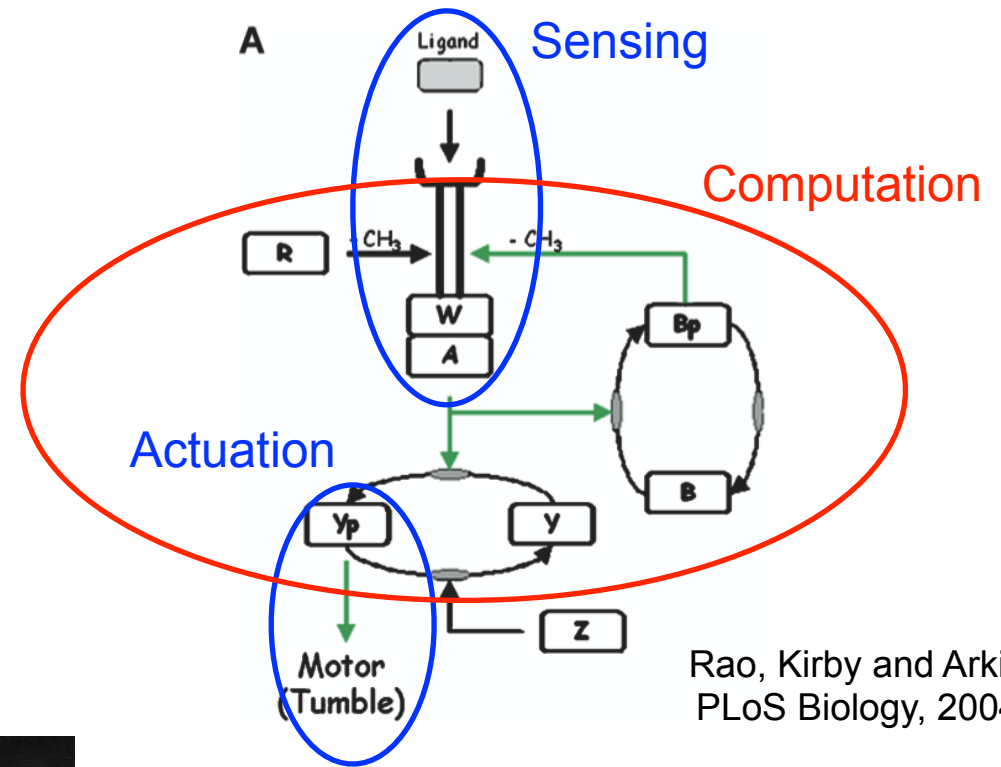
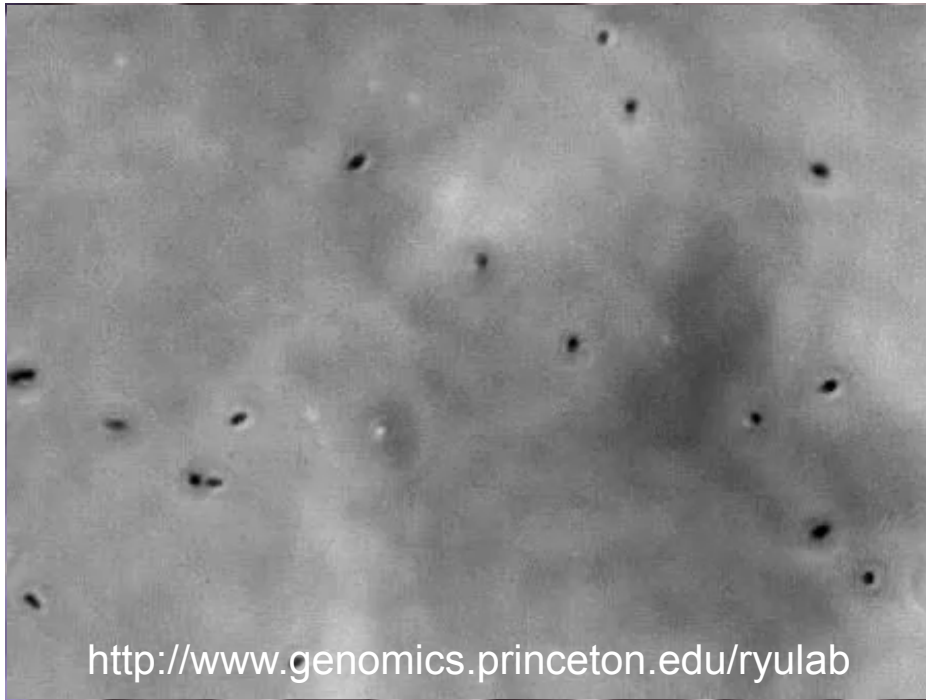
**Richard M. Murray**

Control & Dynamical Systems / Bioengineering  
California Institute of Technology

**34th Chinese Control Conference and SICE Annual Conference 2015**  
**30 July 2015**

Emzo de los Santos (BE) Victoria Hsiao (BE)  
Yutaka Hori (CMS) Zach Sun (MD/PhD) Enoch Yeung (CDS)  
Henrike Niederholtmeyer, Sebastian Maerkl (EPFL)

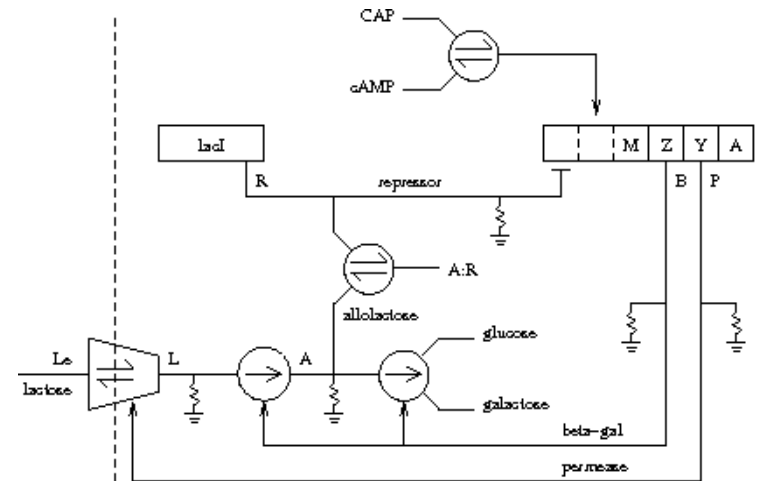
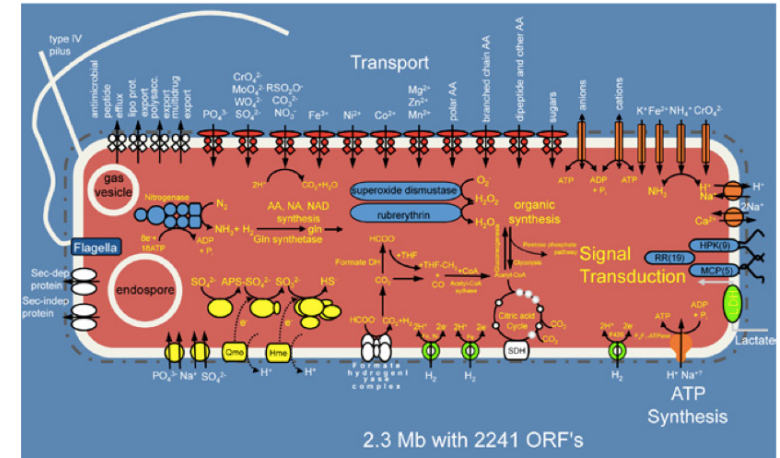
# Feedback Systems in Biology



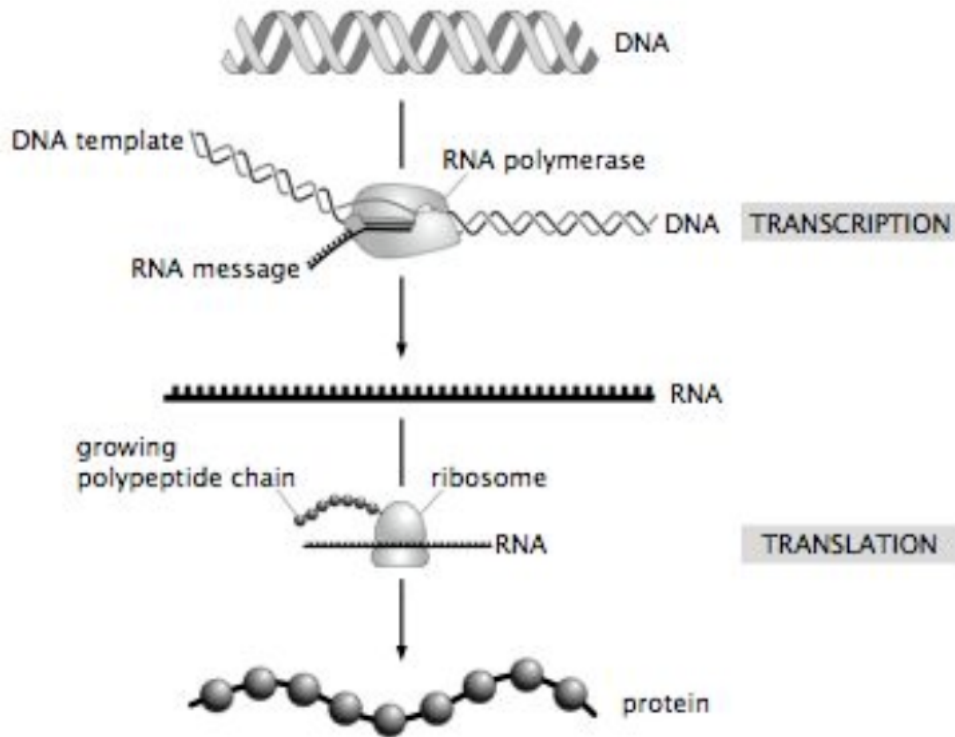
# Outline

Goal for the talk: explain what synthetic biology is about and the role that systems and control theory might play

1. Brief tutorial on biology and synthetic biology
2. Some recent results on design of biomolecular feedback circuits
  - Concentration tracking (Hsiao, de los Santos et al, ACS Syn Bio, 2014)
  - Biomolecular event detectors (Hsiao, Hori et al, work in progress)
  - Biomolecular oscillators (Niederholtmeyer, Sun et al, submitted)
3. Opportunities for the systems and control community



# Central Dogma: DNA to Proteins

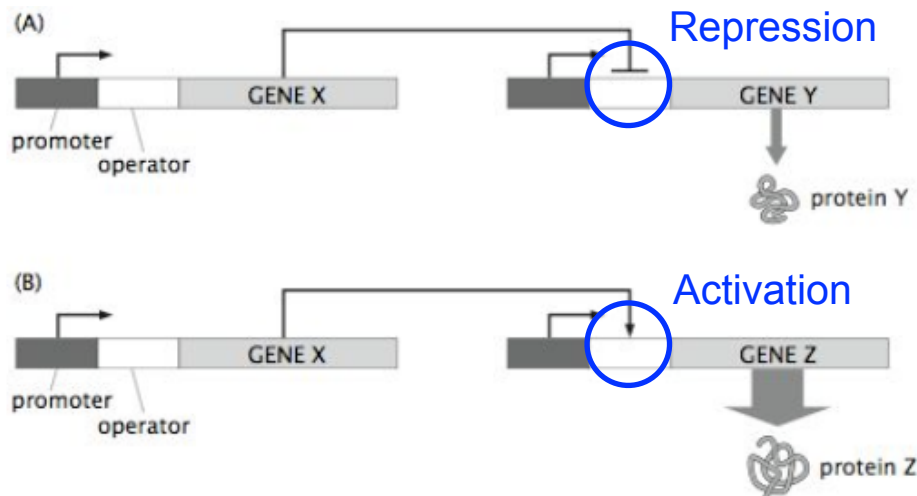


## Transcription: DNA to mRNA

- Double stranded DNA contains nucleotide sequence (A, C, T, G) on a sugar (deoxyribose) backbone
- Watson-Crick pairing: A:T, C:G
- RNA polymerase transcribes DNA sequence to RNA sequence (A, C, U, G sequence on a ribose backbond)

## Translation: mRNA to protein

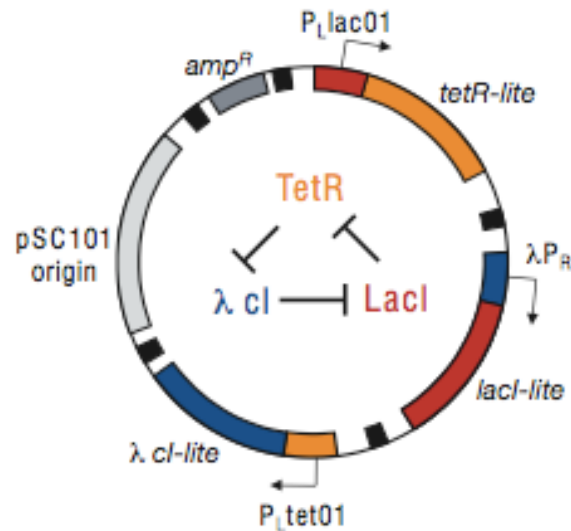
- mRNA is translated by ribosomes into a chain of amino acids using the genetic code (3 bp code for 1 aa)
- Amino acid chain (polypeptide chain) folds into a protein



## Regulation: control of gene expression

- Proteins bind to DNA, RNA and proteins to modulate gene expression
- Repression: X turns off expression of Y
- Activation: X turns on expression of Z

# Biological Circuit Design (Synthetic Biology)

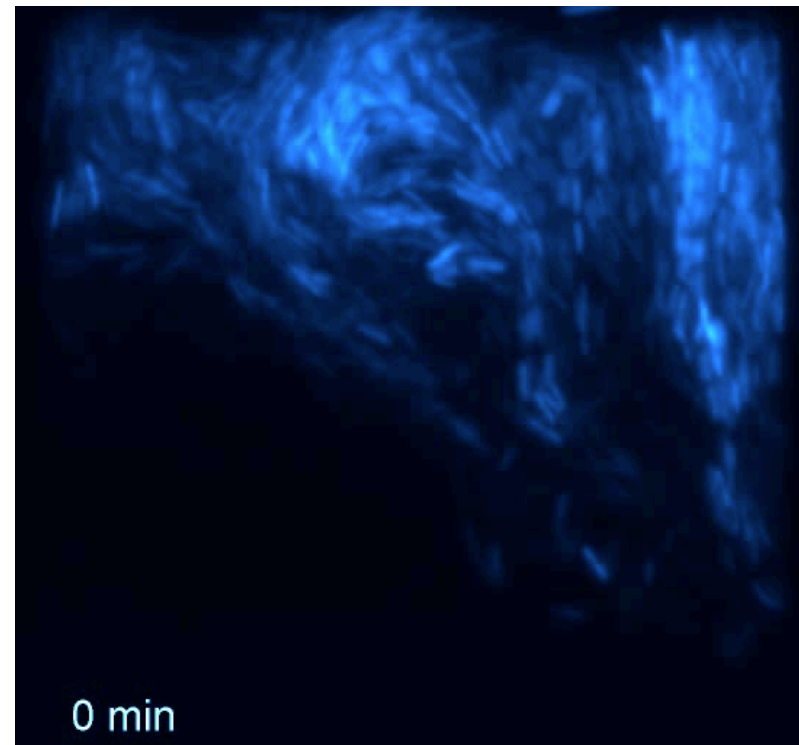


## Repressilator (Elowitz & Leibler; 2000)

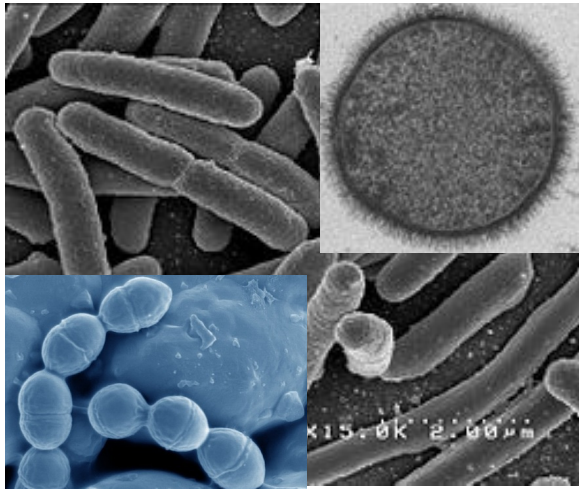
- Ring oscillator with three repressors in a cycle
- Provides oscillations at frequency comparable to cell cycle

## Synchronized oscillators (Danino, Mondragon-Palomino et al, 2010)

- Coupled oscillators by using cell-cell signaling
- Used relaxation style oscillator built on coupled +/- feedback loops + delay

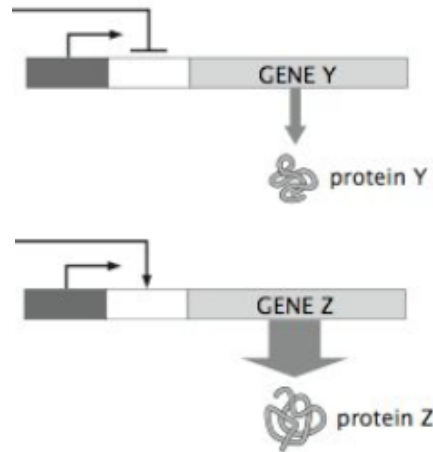


# How Synthetic Biology Works

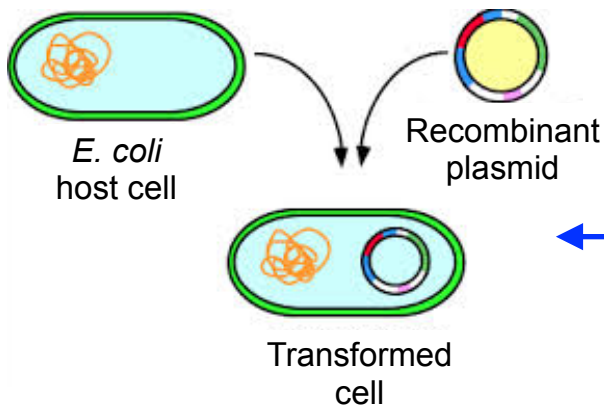
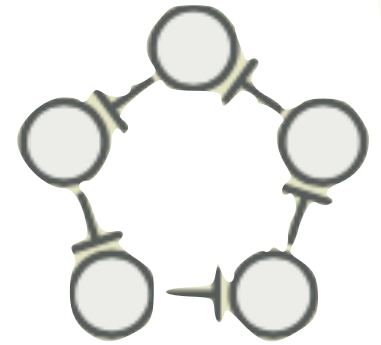


Natural organisms

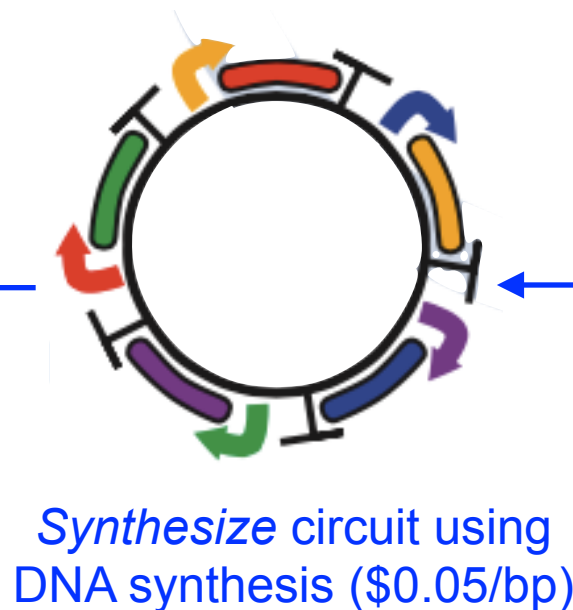
Mine "parts"



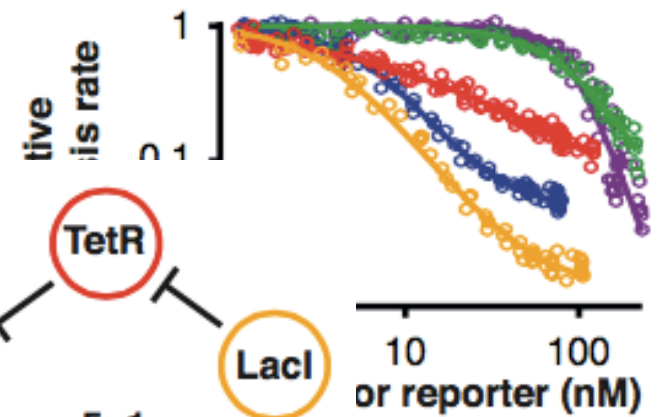
Conceive new circuits



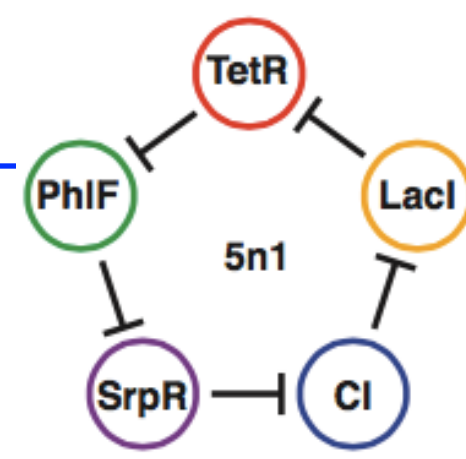
Transform circuit (plasmid) into cells



Synthesize circuit using DNA synthesis (\$0.05/bp)

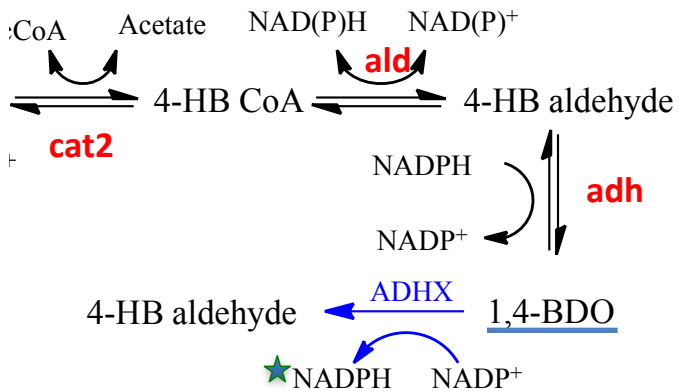


Characterize and choose specific parts to use in circuit



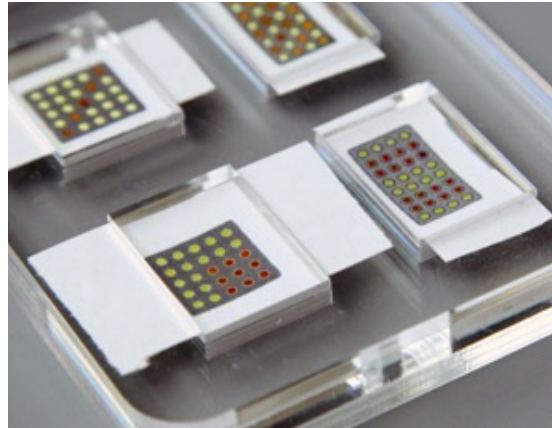
# Synthetic Biology Applications

## Materials Synthesis



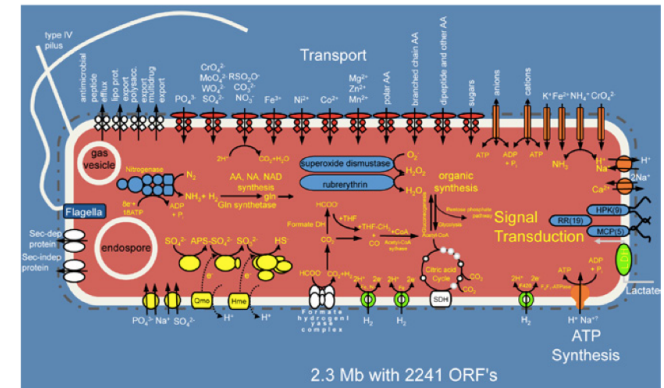
- Conversion of input resources to output products in modular way

## Event Detectors



- Detection of environmental signals at the molecular scale

## Artificial Cells



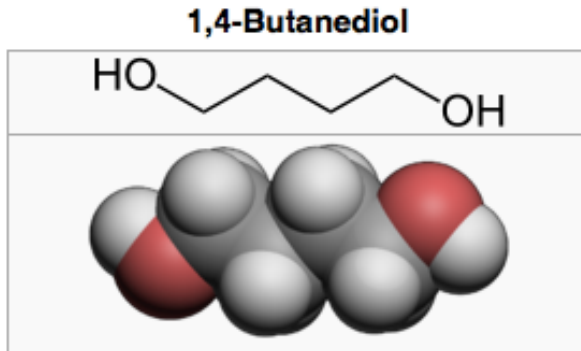
- Self-contained nanoscale biomolecular *machines* (circuits, subsystems, etc)

## Potential Markets for Synthetic Biology Products

- Bio-based chemicals (“green” chemistry): \$4B
- Bio-defense (molecular detection): \$7B
- Therapeutics (health/medicine): \$140B
- Nanoscale robotics: \$0 (today...)



# Materials Synthesis Example: 1,4-BDO

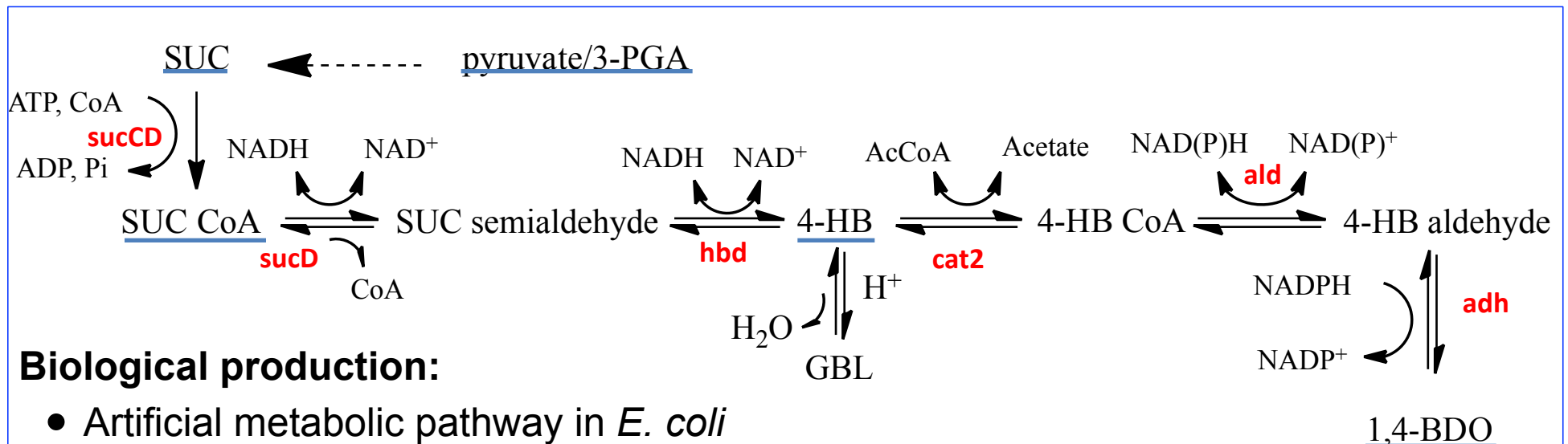
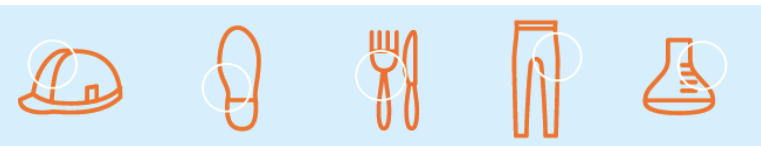


**Industrial solvent used in manufacture plastics, elastic fibers and polyurethanes**

- World production: one million metric tons per year
- Market price is about \$2,000 USD per ton (2005)
- Sample usage: Spandex

**Chemical production:**

- Propylene oxide → allyl alcohol → 4-hydroxybutyraldehyde → 1,4-butanediol



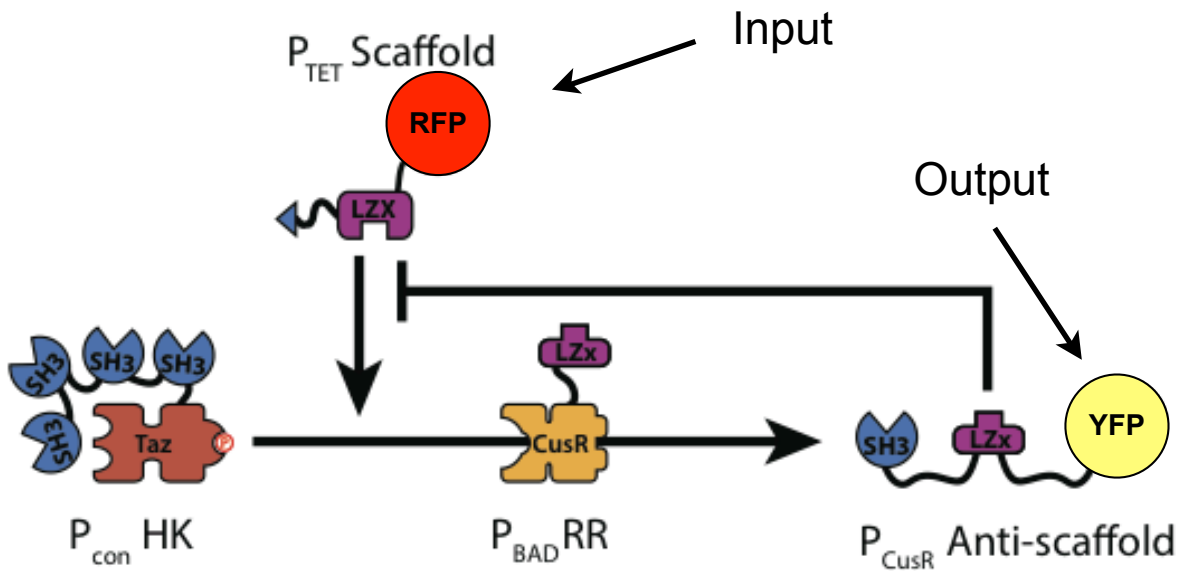
**Biological production:**

- Artificial metabolic pathway in *E. coli*
- Requires enzyme, strain, expression engineering

1,4-BDO

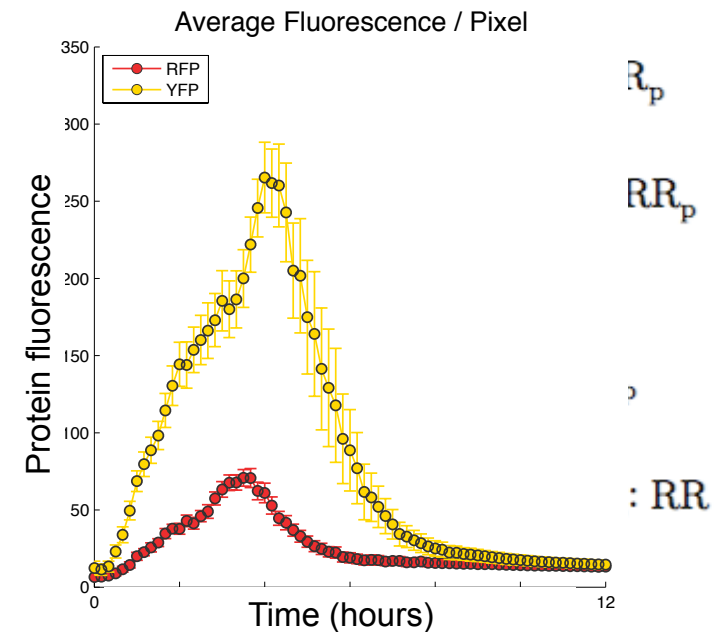
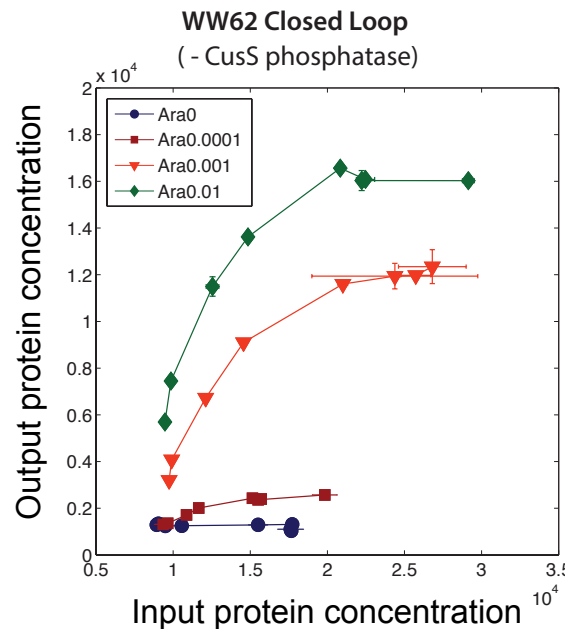
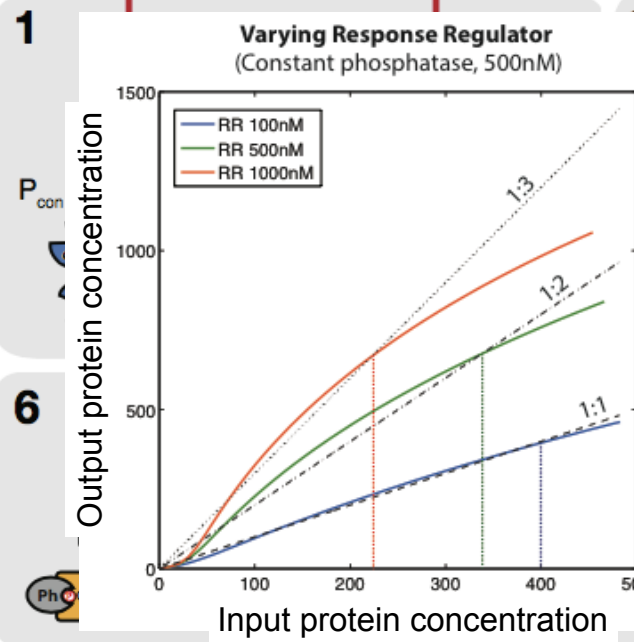


# Concentration Regulation via Scaffold Proteins

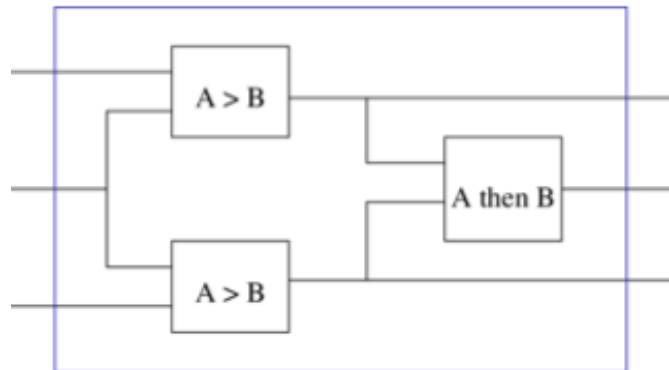
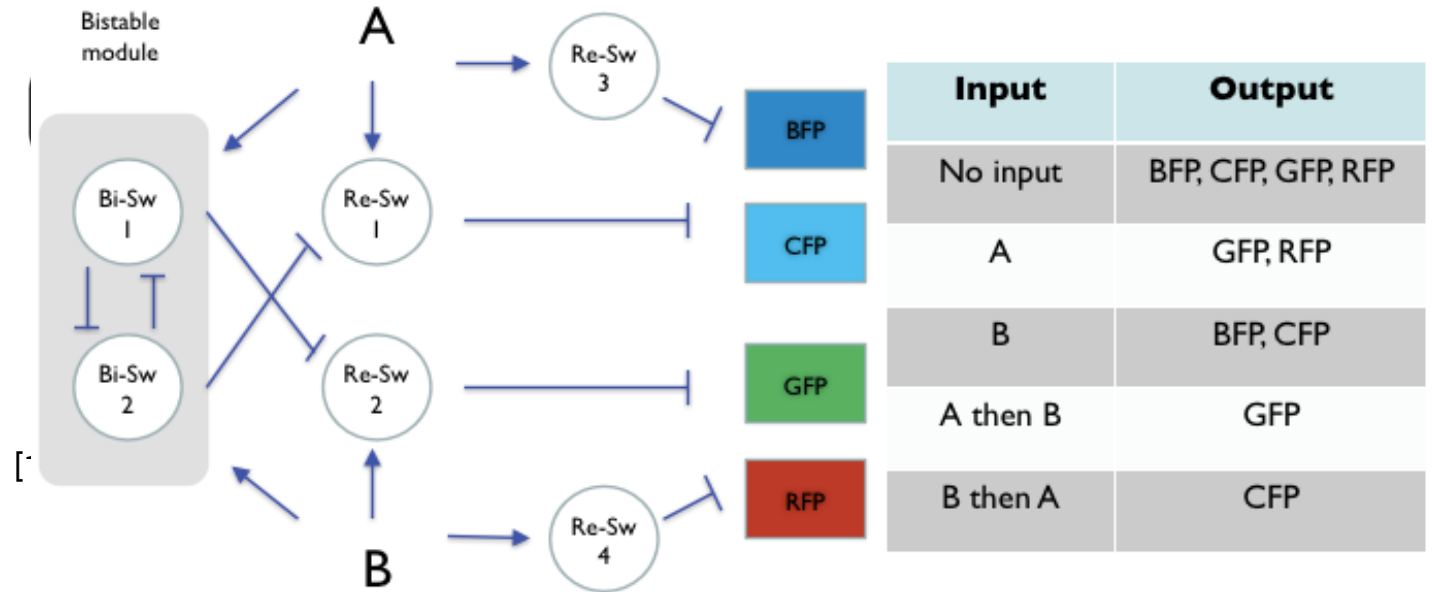
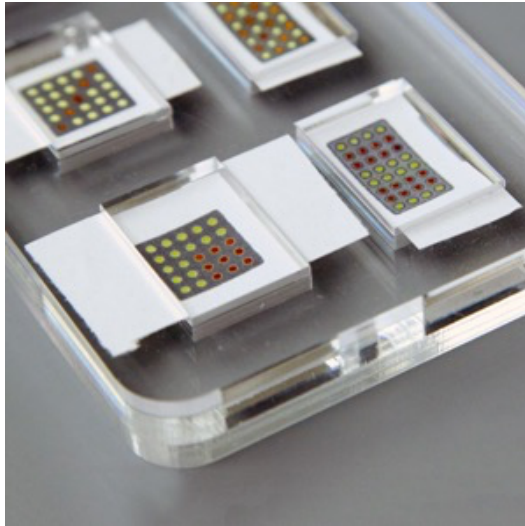


## Circuit operation

- Use scaffold domains to modulate activity of (non-cognate) histidine kinase and response regulator proteins
- Use anti-scaffold feedback to modulate activity level and regulate concentration of output to match input



# Biomolecular Event Detectors



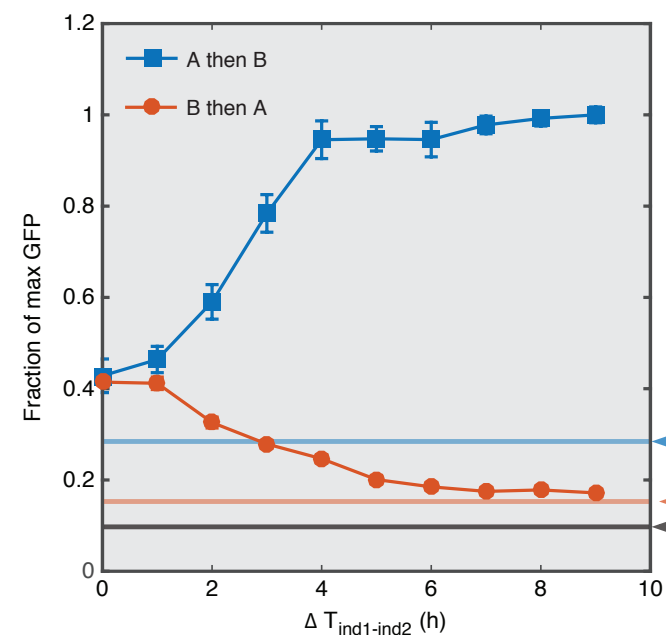
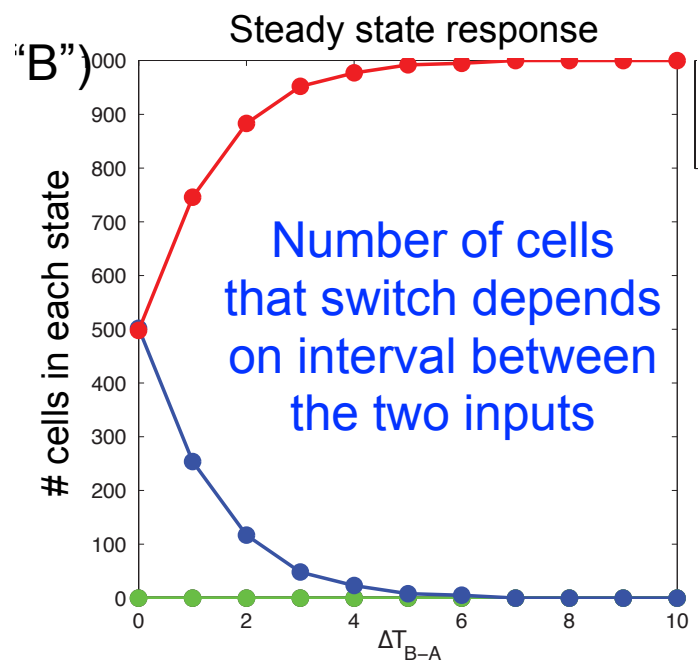
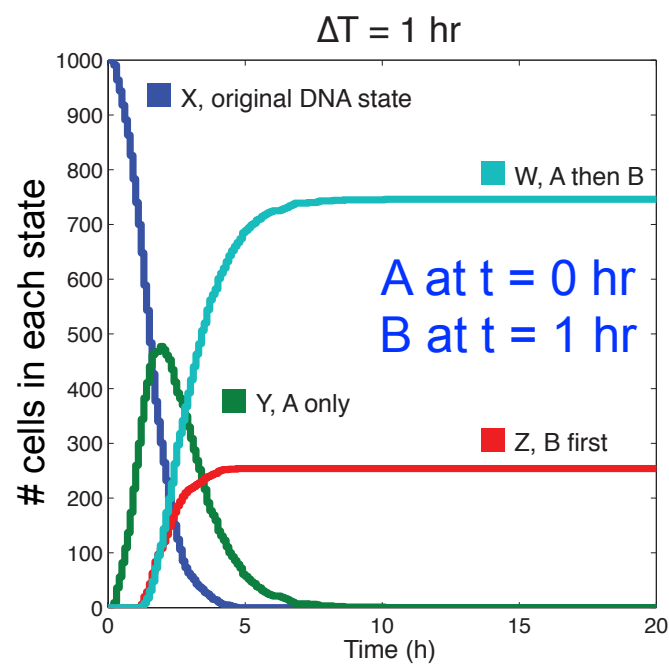
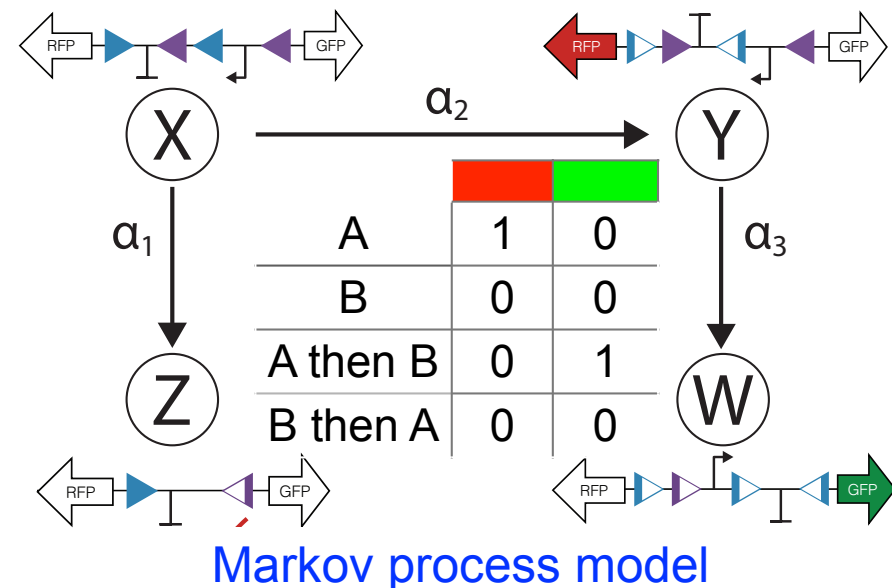
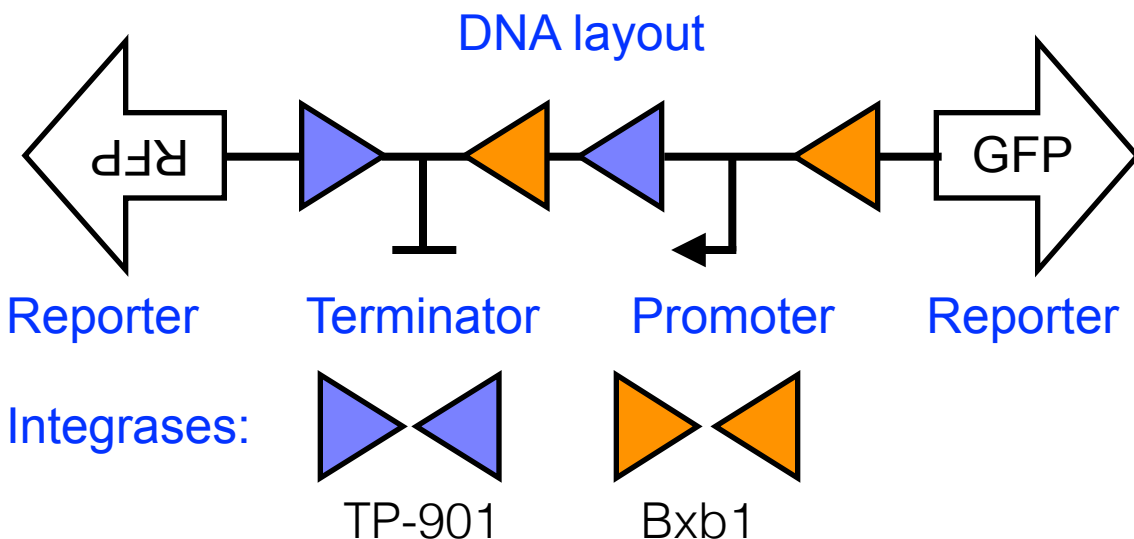
Interconnection of modules to detect more complex events

## Approach

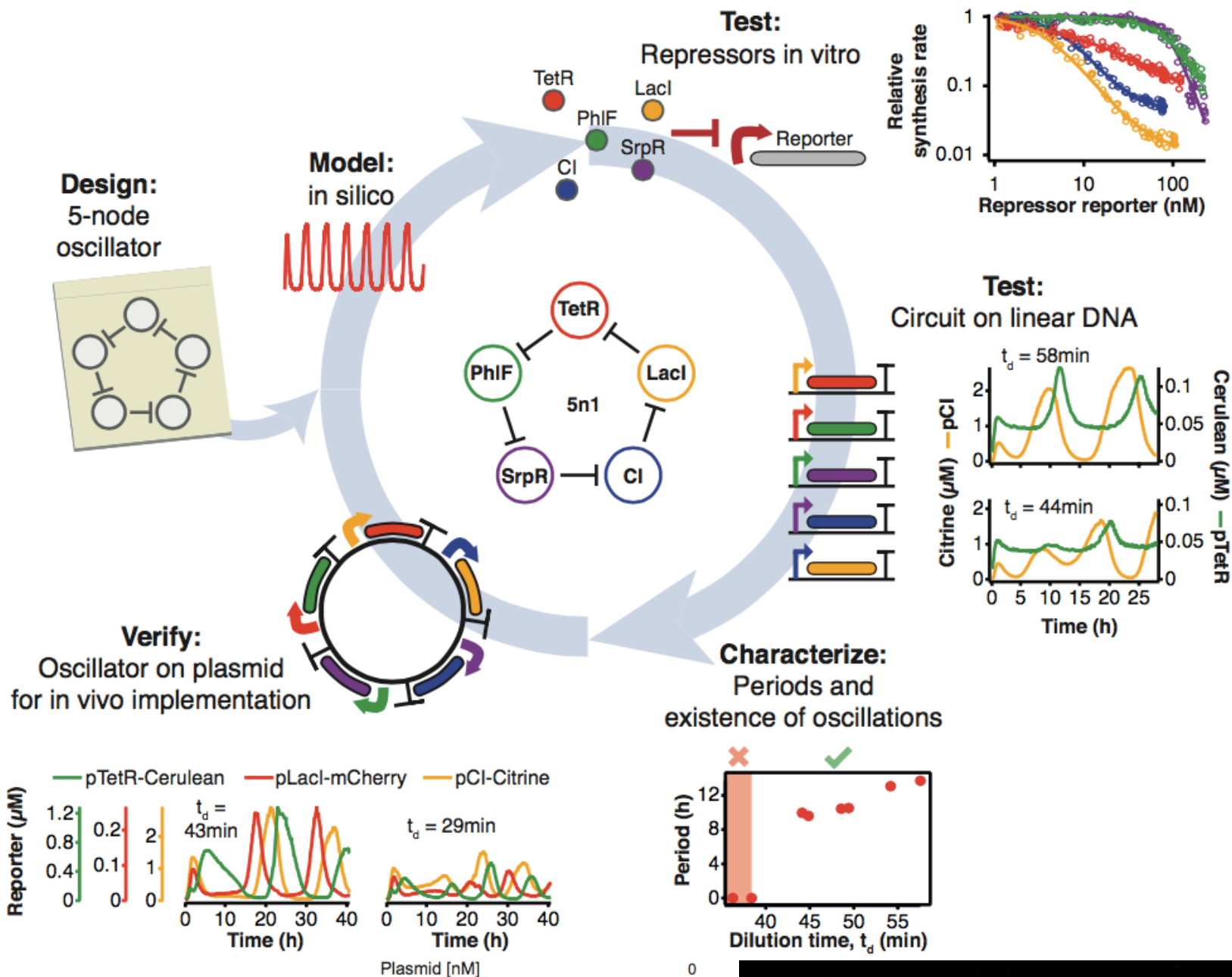
- Component technologies: signal detection, event memory, species comparison, logic functions
- Primitives:  $A > B$ , A followed by B,  $A > \text{thresh}$ , etc
- Interconnection framework: modular techniques for interconnecting components & detectors

**Deployment: paper, hydrogels, cells...**

# Event Ordering Detection (A then B)

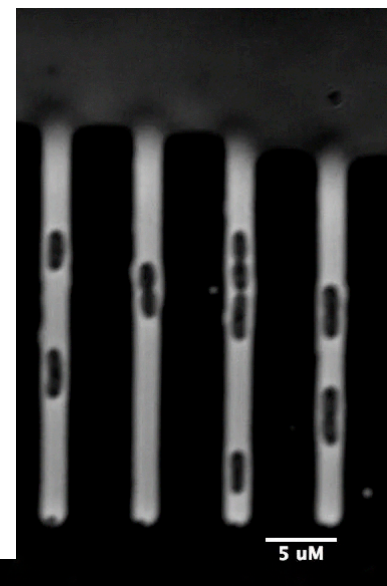


# 5 Node Oscillator Design Cycle



## Timeline:

- 20 Jul: design start
- 24 Jul (4d): *in vitro* demo
- 23 Sep (2m): initial *in vivo*
- 30 Mar (6m): final *in vivo*
- 20 Apr (9m): submit/post



# Control Theory for Biological Systems



1100 5/1/00

<http://www.cds.caltech.edu/~murray/BFS>  
(free PDF download for CCC/SICE'15)

## What's different about biomolecular feedback systems

- Complexity
- Stochasticity
- Communications (and crosstalk)
- Resource limits
- Uncertainty (components and context)
- Evolvability

## Potential application areas for tools from feedback control theory

- System identification
- Analysis (performance, robustness)
- Design (robustness, dynamics, interconnection, modularity)
- Fundamental limits

## Many ways to get started!

- iGEM (undergraduate competition)
- CSHL Syn Bio course (2 wks, summer)